

# Testing Inert Doublet at Future $e^+e^-$ Colliders

Dorota Sokołowska

International Institute of Physics,  
Universidade Federal do Rio Grande do Norte, Natal, Brazil

**DARKWIN: Dark Matter and Weak Interactions Conference**  
**Natal, Brazil, 02-13.09.2019**

based on

**JHEP12(2018)081, JHEP1907(2019)053**  
**and work in progress**

J. Kalinowski, J. Klamka, P. Sopicki, A.F. Żarnecki (University of Warsaw),  
W. Kotlarski (TU Dresden),  
T. Robens (Rudjer Boskovic Institute Zagreb)

## Motivation

- **Standard Model:**

- Higgs particle found at the LHC in 2012
  - very SM-like
- no signal for New Physics as of 2019
- several issues are still not explained by the SM

- **Dark Matter:**

- if Standard Cosmological Model correct: 85% mass missing
- only gravitational interaction observed
- no (in)direct detection signal
- nature of DM unknown – here we assume it is a WIMP
- complementary approach preferred for testing DM models
- here we focus on  $e^+e^-$  colliders

# Outline

## Inert Doublet Model

- particle content and parameters
- experimental and theoretical constraints
- benchmarks

## Inert Scalars at Linear Colliders

- low-energy stages of ILC and CLIC
- high-energy stages of CLIC
- semi-leptonic channels at 3 TeV CLIC

## Inert Doublet Model

2-Higgs Doublet Model with an exact  $Z_2$  symmetry

$$\Phi_S = \left( \begin{array}{c} G^\pm \\ \frac{v+h+iG^0}{\sqrt{2}} \end{array} \right), \Phi_D = \left( \begin{array}{c} H^\pm \\ \frac{H+iA}{\sqrt{2}} \end{array} \right)$$

- $\Phi_S$  is the **SM-like Higgs** doublet, with the SM-like Higgs  $h$
- $\Phi_D$  (**inert doublet**) has four additional scalars  $H, A, H^\pm$ ,
- a discrete  $Z_2$  symmetry:
  - $\Phi_S$  is *even*:  $\Phi_S \rightarrow \Phi_S$  (also SM $\rightarrow$ SM)
  - $\Phi_D$  is *odd*:  $\Phi_D \rightarrow -\Phi_D$ ,
- Yukawa-type interactions only for Higgs doublet ( $\Phi_S$ ):
  - $\Phi_D$  **does not interact with the SM fermions**
- the lightest inert particle is stable: a natural **candidate for DM**
- we assume  $H$  is the DM particle

$$M_H < M_A, M_{H^\pm}$$

## Parameters

- The model contains seven free parameters

$$\lambda_{1,2,3,4,5}, m_{11}^2, m_{22}^2$$

- after EWSB  $\lambda_1, m_{11}^2$  fixed from the SM ( $v, M_h$ )
- left with **five free parameters**, which we take as:
  - three inert scalar masses:  $M_H, M_A, M_{H^\pm}$
  - two couplings,  $\lambda_2$  and  $\lambda_{345} = \lambda_3 + \lambda_4 + \lambda_5$
- inert scalars' couplings to  $\gamma, W^\pm$  and  $Z$  determined by SM parameters

We scanned the IDM parameter space looking for scenarios consistent with current **theoretical** and **experimental constraints**, for masses up to 1 TeV.

Details in *Benchmarking the Inert Doublet Model for  $e^+e^-$  colliders*  
JHEP12(2018)081 [arXiv:1809.07712]

## Parameter Scan

- **Positivity of potential:**

$$\lambda_1 > 0, \lambda_2 > 0, \lambda_3 + \sqrt{\lambda_1 \lambda_2} > 0, \lambda_{345} + \sqrt{\lambda_1 \lambda_2} > 0.$$

- **Perturbativity:**

$$\lambda_i \leq 4\pi$$

- **Global minimum:**

$$\frac{m_{11}^2}{\sqrt{\lambda_1}} \geq \frac{m_{22}^2}{\sqrt{\lambda_2}}$$

- **LEP bound on charged scalar:**

$$M_{H^\pm} \geq 70 \text{ GeV}$$

- **Recast LEP searches for SUSY particles:**

$$M_A \leq 100 \text{ GeV}, M_H \leq 80 \text{ GeV}, \Delta M(A, H) \geq 8 \text{ GeV},$$

- **$H$  is the lightest inert scalar:**

$$M_H < M_A, M_H^\pm$$

- **Higgs mass from the LHC:**

$$M_h = 125.1 \text{ GeV}$$

## Parameter Scan: Step 1

Step 1 - done using 2HDMC

- **Unitarity:**

the scalar  $2 \rightarrow 2$  scattering matrix should be unitary

- **Higgs total decay width:**

$$\Gamma_{tot} \leq 9\text{MeV}$$

- **No EW bosons decays:**

$$M_{A,H} + M_{H^\pm} \geq M_W, M_A + M_H \geq M_Z, 2 M_{H^\pm} \geq M_Z$$

- **EWPT:**

$2\sigma$  (i.e. 95% C.L.) agreement with electroweak precision observables

- **No long-lived charged scalars:**

$$\tau_{H^\pm} \leq 10^{-7} \text{ s} \Rightarrow \Gamma_{H^\pm} \geq 6.58 \times 10^{-18} \text{ GeV}$$

## Parameter Scan: Step 2 and 3

**Step 2** – done using `HiggsSignals`, `HiggsBounds`:

- Higgs invisible decays
- $h \rightarrow \gamma\gamma$  signal strength and other
- reinterpreted direct (null) searches for BSM physics

**Step 3** – done using `micrOMEGAs`:

- DM relic density – upper Planck limit:

$$\Omega_H h^2 \leq \Omega_{DM} h^2 = 0.1224$$

- $\Omega_H h^2 = \Omega_{DM} h^2$  if possible
- direct detection – latest results from XENON1T (2018)
- indirect detection – no new exclusions for most points



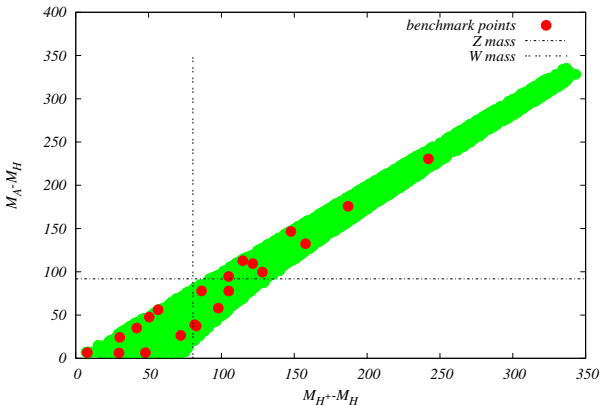
## Constraints for $M_H$

- $M_H \leq 45$  GeV:  
**excluded** by at least one of  $Br(h \rightarrow inv), \Gamma_{W,Z}, \Omega_{DM}h^2$   
Larger DM masses are still viable:
- $45 \text{ GeV} < M_H \lesssim 57 \text{ GeV}$ :  
OK but  $\Omega_H h^2 < \Omega_{DM} h^2$
- $57 \text{ GeV} \lesssim M_H \lesssim 75 \text{ GeV}$ :  
OK and  $\Omega_H h^2 \leq \Omega_{DM} h^2$  (100% DM possible)
- $75 \text{ GeV} \lesssim M_H \lesssim 525 \text{ GeV}$ :  
OK but  $\Omega_H h^2 < \Omega_{DM} h^2$
- $M_H \gtrsim 525 \text{ GeV}$ :  
OK and  $\Omega_H h^2 \leq \Omega_{DM} h^2$  (100% DM possible)

Constraints for  $M_A, M_{H^\pm}$ 

- from EWPT:

$$M_A < M_{H^\pm} \text{ and } M_{H^\pm} - M_A \lesssim 70 \text{ GeV}$$



- if exact relic density for heavy masses then masses almost degenerated

## Constrains for $\lambda_2, \lambda_{345}$

### self-coupling $\lambda_2$

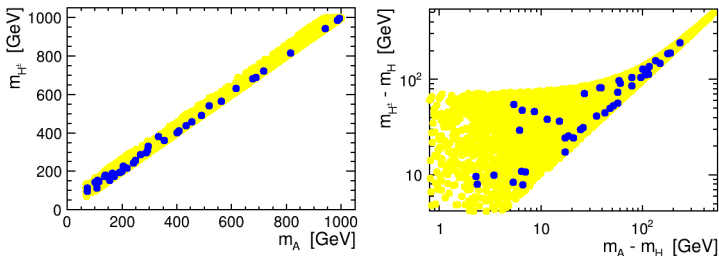
- direct constraints from positivity, perturbative unitarity
- no influence on tree-level DM annihilation, LHC physics
- possible test – self-interaction of DM? loop corrections?

### Higgs-DM coupling $\lambda_{345}$

- very strong constraints from LHC & DD & relic density
- $\lambda_{345} \sim \mathcal{O}(10^{-3})$
- after that almost no influence on collider physics
- not relevant at LC

## IDM benchmark points

- about 15000 points consistent with all considered constraints found
- 41 points (21 accessible at 500 GeV) chosen for detailed study



The selection was arbitrary, but we tried to

- cover a wide range of scalar masses and mass splittings
- get significant contribution to the relic density

*Detailed list of parameters for all benchmarks: backup slides*

## Significance of mass splittings

BP1 and BP6:

	$M_H$	$M_A$	$M_{H^\pm}$	$V$ or $V^*$
BP1	72.77	107.8	114.6	$Z^*, W^{\pm*}$
BP6	72.14	109.5	154.8	$Z^*, W^\pm$

BP8 and BP15:

	$M_H$	$M_A$	$M_{H^\pm}$	$V$ or $V^*$
BP8	70.91	148.7	175.9	$Z^*, W^\pm$
BP15	71.03	217.7	218.7	$Z, W^\pm$

On-shell scalar production for  $\sqrt{s} = 250, 380, 500$  GeV $\sigma(e^+e^- \rightarrow H^+H^-)$  [fb] $\sigma(e^+e^- \rightarrow AH)$  [fb]

	$\sigma(250)$	$\sigma(380)$	$\sigma(500)$		$\sigma(250)$	$\sigma(380)$	$\sigma(500)$
BP1	23.7	97.8	82.6	BP8	20	47.5	38.1
BP6	-	33.3	53.2	BP15	-	18.2	24.2

main decay channels:  $H^\pm \rightarrow HW^{\pm(*)}, A \rightarrow HZ^{(*)}$

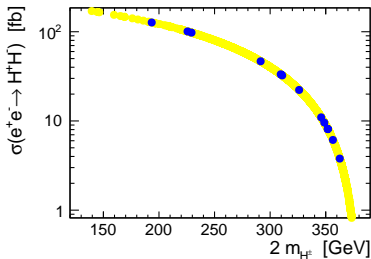
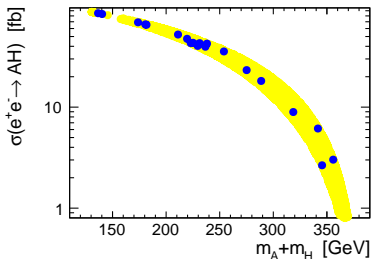
## Scalar production at $e^+e^-$ colliders

Production of IDM scalars is dominated by two processes:

$$e^+e^- \rightarrow A H$$

$$e^+e^- \rightarrow H^+ H^-$$

Leading-order cross sections:



(plots for  $\sqrt{s} = 380$  GeV (1st stage CLIC))

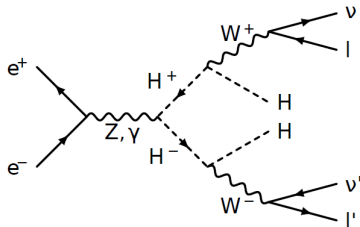
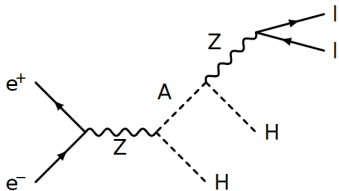
# Signatures

*AH* production process followed by the *A* decay  $\rightarrow$  lepton pair production:

$$e^+e^- \rightarrow HA \rightarrow HHZ^{(*)} \rightarrow HH\mu^+\mu^-,$$

$H^+H^-$  production with decaying  $H^\pm \rightarrow$  different flavour lepton pair:

$$e^+e^- \rightarrow H^+H^- \rightarrow HHW^{+(*)}W^{-(*)} \rightarrow HHl^+l'^-\nu\bar{\nu}'$$



## Signal processes

We consider two possible final state signatures:

- **muon pair production**,  $\mu^+\mu^-$ , mainly from  $HA$
- **electron-muon pair production**,  $\mu^+e^-$  or  $e^+\mu^-$ , mainly from  $H^+H^-$
- both channels include contributions from  $AH$  and  $H^+H^-$  production

Signal processes for  $\mu^+\mu^-$  final state (with  $\tau^\pm \rightarrow \mu^\pm\nu\nu$ )

$$\begin{aligned}
 e^+e^- &\rightarrow \mu^+\mu^- HH, \\
 &\rightarrow \mu^+\mu^- \nu_\mu \bar{\nu}_\mu HH, \\
 &\rightarrow \tau^+\mu^- \nu_\tau \bar{\nu}_\mu HH, \quad \mu^+\tau^- \nu_\mu \bar{\nu}_\tau HH, \\
 &\rightarrow \tau^+\tau^- HH, \quad \tau^+\tau^- \nu_\tau \bar{\nu}_\tau HH.
 \end{aligned}$$

Signal processes for  $e^\pm\mu^\mp$  final state (with  $\tau^\pm \rightarrow \mu^\pm\nu\nu, e^\pm\nu\nu$ )

$$\begin{aligned}
 e^+e^- &\rightarrow \mu^+\nu_\mu e^- \bar{\nu}_e HH, \quad e^+\nu_e \mu^- \bar{\nu}_\mu HH, \\
 &\rightarrow \mu^+\nu_\mu \tau^- \bar{\nu}_\tau HH, \quad \tau^+\nu_\tau \mu^- \bar{\nu}_\mu HH, \\
 &\rightarrow e^+\nu_e \tau^- \bar{\nu}_\tau HH, \quad \tau^+\nu_\tau e^- \bar{\nu}_e HH, \\
 &\rightarrow \tau^+\tau^- HH, \quad \tau^+\nu_\tau \tau^- \bar{\nu}_\tau HH,
 \end{aligned}$$



## Analysis strategy

Tools used:

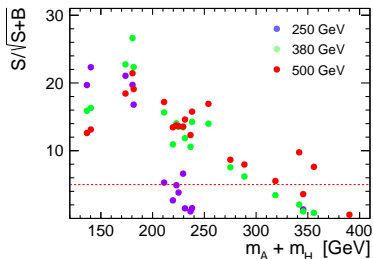
- signal and background samples from WHizard 2.2.8
- based on dedicated IDM model implementation in SARAH
- parameter files for benchmark scenarios from SPheno 4.0.3
- Boosted Decision Tree classification algorithm in TMVA toolkit
- BDT classifier with 8 input variables used for selection of signal events

Analysis for CLIC in *Exploring Inert Scalars at CLIC* (arXiv:1811.06952),  
*The CLIC Potential for New Physics* (arXiv:1812.02093)

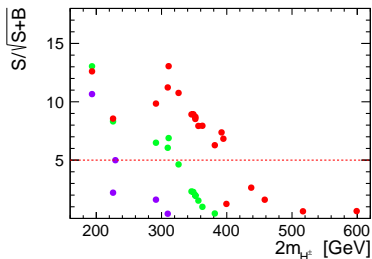
$$\sqrt{s} = 250, 380, 500 \text{ GeV}$$

Depending on the scalar masses, many benchmarks are already accessible at first stages of ILC and CLIC:

$AH$  signature ( $\mu^+\mu^-$ )



$H^+H^-$  signature ( $\mu^\pm e^\mp$ )



for all  $\sqrt{s}$  we take  $1000 \text{ fb}^{-1}$

Discovery reach for  $\sqrt{s} = 250, 380, 500 \text{ GeV}$ :

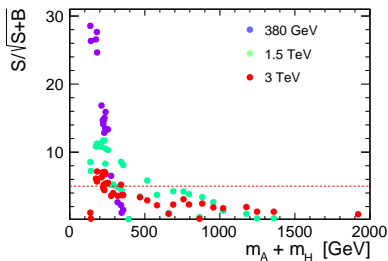
- neutral scalar production:  $M_A + M_H < 220, 300, 360 \text{ GeV}$
- charged scalar production:  $M_{H^\pm} < 110, 160, 200 \text{ GeV}$

$$\sqrt{s} = 1.5, 3 \text{ TeV}$$

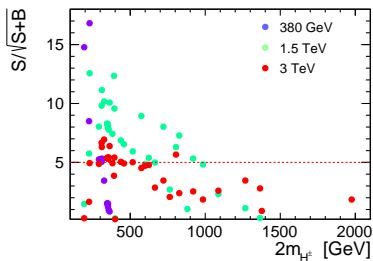
Same analysis procedure applied for CLIC Stage 2 & 3:

2500 fb<sup>-1</sup> at 1.5 TeV and 5000 fb<sup>-1</sup> at 3 TeV

*AH* signature ( $\mu^+\mu^-$ )



*H<sup>+</sup>H<sup>-</sup>* signature ( $\mu^\pm e^\mp$ )

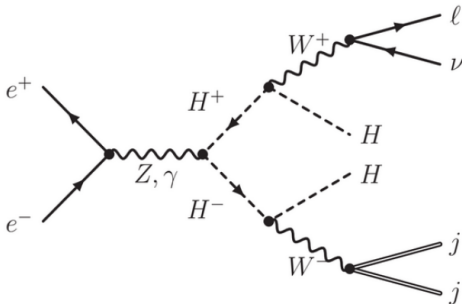


Moderate increase in discovery reach for 1.5 TeV:

- neutral scalar production:  $M_A + M_H < 550 \text{ GeV}$  (360 GeV @ 500 GeV)
- charged scalar production:  $M_{H^\pm} < 500 \text{ GeV}$  (200 GeV @ 500 GeV)

No significant gain from going to 3 TeV.

## Semi-leptonic channels



Main SM background:  $qq\ell\nu, qq\ell\ell$

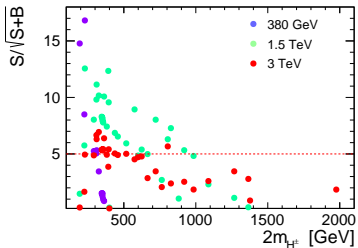
- significantly larger branching ratio:

$$\text{Br}(W^\pm \rightarrow \ell\nu) \approx 2\%, \quad \text{Br}(W^\pm \rightarrow qq) \approx 20\%$$

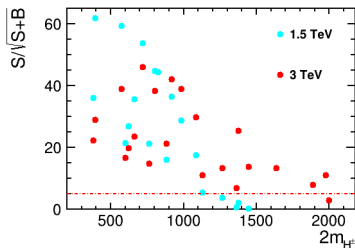
- leads to larger cross-sections!

## Semi-leptonic channels

Leptonic signature



Semi-leptonic signature



- significant improvement compared to leptonic channels
- only one benchmark with very small  $M_{H^\pm} - M_H$  still inaccessible

## Summary

- The IDM – a simple model with rich phenomenology
- $e^+e^-$  colliders can test large part of the parameter space
- Low mass scenarios can be observed with high significance in the di-muon channel already at the low energy stages of CLIC and ILC, up to  $M_A + M_H \sim 360 \text{ GeV}$  and  $M_{H^\pm} \sim 200 \text{ GeV}$
- The discovery reach is extended to  $\sim 500 \text{ GeV}$  when running at 1.5 TeV
- No real improvement in leptonic channels with 3 TeV run
- For semi-leptonic channel significant increase in discovery reach

# Backup slides

## Low mass IDM benchmark points

No.	$M_H$	$M_A$	$M_{H^\pm}$	$\lambda_2$	$\lambda_{345}$	$\Omega_H h^2$
<b>BP1</b>	72.77	107.8	114.6	1.445	-0.004407	0.1201
BP2	65	71.53	112.8	0.7791	0.0004	0.07081
BP3	67.07	73.22	96.73	0	0.00738	0.06162
BP4	73.68	100.1	145.7	2.086	-0.004407	0.08925
<b>BP6</b>	72.14	109.5	154.8	0.01257	-0.00234	0.1171
BP7	76.55	134.6	174.4	1.948	0.0044	0.0314
<b>BP8</b>	70.91	148.7	175.9	0.4398	0.0051	0.124
BP9	56.78	166.2	178.2	0.5027	0.00338	0.08127
BP10	76.69	154.6	163	3.921	0.0096	0.02814
BP11	98.88	155	155.4	1.181	-0.0628	0.002737
BP12	58.31	171.1	173	0.5404	0.00762	0.00641
BP13	99.65	138.5	181.3	2.463	0.0532	0.001255
<b>BP14</b>	71.03	165.6	176	0.3393	0.00596	0.1184
<b>BP15</b>	71.03	217.7	218.7	0.7665	0.00214	0.1222
<b>BP16</b>	71.33	203.8	229.1	1.03	-0.00122	0.1221
BP18	147	194.6	197.4	0.387	-0.018	0.001772
BP19	165.8	190.1	196	2.768	-0.004	0.002841
BP20	191.8	198.4	199.7	1.508	0.008	0.008494
<b>BP21</b>	57.48	288	299.5	0.9299	0.00192	0.1195
<b>BP22</b>	71.42	247.2	258.4	1.043	-0.00406	0.1243
BP23	62.69	162.4	190.8	2.639	0.0056	0.06404



## High mass IDM benchmark points

No.	$M_H$	$M_A$	$M_{H^\pm}$	$\lambda_2$	$\lambda_{345}$	$\Omega_H h^2$
HP1	176	291.4	312	1.49	-0.1035	0.0007216
HP2	557	562.3	565.4	4.045	-0.1385	0.07209
HP3	560	616.3	633.5	3.38	-0.0895	0.001129
HP4	571	676.5	682.5	1.98	-0.471	0.0005635
HP5	671	688.1	688.4	1.377	-0.1455	0.02447
HP6	713	716.4	723	2.88	0.2885	0.03515
HP7	807	813.4	818	3.667	0.299	0.03239
HP8	933	940	943.8	2.974	-0.2435	0.09639
HP9	935	986.2	988	2.484	-0.5795	0.002796
<b>HP10</b>	990	992.4	998.1	3.334	-0.051	0.1248
HP11	250.5	265.5	287.2	3.908	-0.1501	0.00535
HP12	286.1	294.6	332.5	3.292	0.1121	0.00277
HP13	336	353.3	360.6	2.488	-0.1064	0.00937
HP14	326.6	331.9	381.8	0.02513	-0.06267	0.00356
HP15	357.6	400	402.6	2.061	-0.2375	0.00346
HP16	387.8	406.1	413.5	0.8168	-0.2083	0.0116
HP17	430.9	433.2	440.6	3.003	0.08299	0.0327
HP18	428.2	454	459.7	3.87	-0.2812	0.00858
HP19	467.9	488.6	492.3	4.122	-0.252	0.0139
HP20	505.2	516.6	543.8	2.538	-0.354	0.00887

## Low mass benchmark points [Points from arXiv:1809.07712]

No.	$M_H$	$M_A$	$M_{H^\pm}$	$HA$	$HH^+$	$AH^+$	$H^+H^-$	AA	onshell
<b>BP1</b>	72.77	107.803	114.639	322	304	169	132	0.4	
BP2	65	71.525	112.85	1022	363	322	140	0.1	
<b>BP3</b>	67.07	73.222	96.73	909	504	444	242	0.1	
BP4	73.68	100.112	145.728	377	165	115	55.1	0.3	
<b>BP6</b>	72.14	109.548	154.761	314	144	88.9	45.1	0.4	W
BP7	76.55	134.563	174.367	173	99.0	50.8	29.2	0.4	W
<b>BP8</b>	70.91	148.664	175.89	144	103	42.7	28.3	0.5	W
BP9	56.78	166.22	178.24	125	116	34.4	27.1	0.6	W, Z
BP10	76.69	154.579	163.045	120	119	46.4	37.3	0.5	W
BP11	98.88	155.037	155.438	87.7	101	50.4	43.8	0.2	
BP12	58.31	171.148	172.96	113	125	34.5	30.3	0.6	W, Z
BP13	99.65	138.484	181.321	113	68.8	44.7	25.2	0.3	W
<b>BP14</b>	71.03	165.604	175.971	106	103	35.5	28.3	0.5	W, Z
<b>BP15</b>	71.03	217.656	218.738	46.9	54.6	14.2	12.8	0.4	W, Z
<b>BP16</b>	71.33	203.796	229.092	57.3	47.3	14.6	10.8	0.4	W, Z
BP18	147	194.647	197.403	29.6	34.0	21.3	17.9	0.1	
BP19	165.8	190.082	195.999	25.5	28.6	22.5	18.3	0.03	
<b>BP20</b>	191.8	198.376	199.721	17.9	21.4	20.1	16.9	0.03	
<b>BP21</b>	57.475	288.031	299.536	20.6	21.8	4.02	4.04	0.3	W, Z
<b>BP22</b>	71.42	247.224	258.382	31.3	32.5	8.05	6.90	0.4	W, Z
BP23	62.69	162.397	190.822	125	88.9	31.3	21.1	0.5	W, Z

## Production cross sections in fb, at 13 TeV [UFO+Madgraph]

&gt; 1000 events in Run II for each process: all but BPs 21 and 22

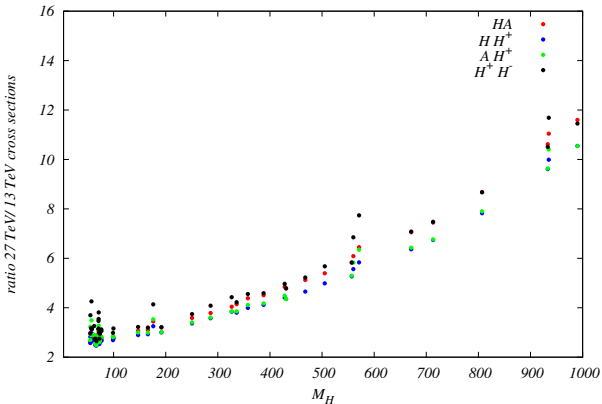
## High mass benchmark points [Points from arXiv:1809.07712]

No.	$M_H$	$M_A$	$M_{H^\pm}$	$HA$	$HH^+$	$AH^+$	$H^+H^-$	$AA$	onshell
<b>HP1</b>	<b>176</b>	<b>291.36</b>	<b>311.96</b>	<b>8.3</b>	<b>8.8</b>	<b>4.0</b>	<b>3.1</b>	<b>0.1</b>	W,Z
HP2	557	562.316	565.417	0.2	0.3	0.3	0.2	-	
HP3	560	616.32	633.48	0.1	0.2	0.2	0.1	0.003	
HP4	571	676.534	682.54	0.1	0.1	0.1	0.08	0.005	W,Z
HP5	671	688.108	688.437	0.07	0.1	0.09	0.07	-	
HP6	713	716.444	723.045	0.05	0.07	0.07	0.05	-	
HP7	807	813.369	818.001	0.03	0.04	0.04	0.03	-	
HP8	933	939.968	943.787	0.01	0.02	0.02	0.01	-	
HP9	935	986.22	987.975	0.009	0.01	0.01	0.009	-	
<b>HP10</b>	990	992.36	998.12	0.07	0.01	0.01	0.008	-	
<b>HP11</b>	<b>250.5</b>	<b>265.49</b>	<b>287.226</b>	<b>5.8</b>	<b>6.3</b>	<b>5.7</b>	<b>4.0</b>	-	
HP12	286.05	294.617	332.457	3.6	3.6	3.4	2.2	0.003	
HP13	336	353.264	360.568	1.7	2.2	2.0	1.5	0.001	
HP14	326.55	331.938	381.773	2.1	2.0	2.0	1.2	-	
HP15	357.6	399.998	402.568	1.1	1.5	1.2	1.0	0.006	
HP16	387.75	406.118	413.464	0.9	1.2	1.1	0.8	-	
HP17	430.95	433.226	440.624	0.6	0.8	0.8	0.6	-	
HP18	428.25	453.979	459.696	0.6	0.8	0.7	0.5	-	
HP19	467.85	488.604	492.329	0.4	0.5	0.5	0.4	-	
HP20	505.2	516.58	543.794	0.3	0.4	0.3	0.2	-	

**Production cross sections in fb, at 13 TeV** [UFO+Madgraph]

> 1000 events at HL-LHC for each process: **HP1, HP11-19**

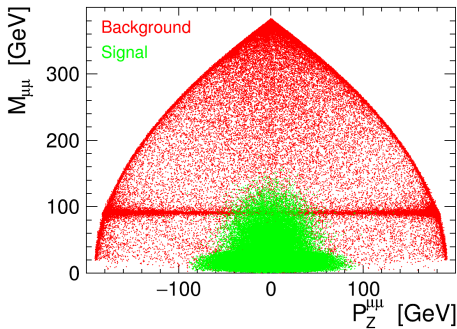
## LHC: 27 TeV vs 13 TeV



**Figure:** Ratio of production cross sections for the four dominant production channels at the 27 TeV HE-LHC and current center-of-mass energy of 13 TeV. While in the low energy range, cross sections are enhanced roughly by a factor  $\lesssim 3$ , for higher masses they can change by an order of magnitude.

## Neutral scalar production @ 380 GeV

Muon pair inv. mass  $M_{\mu\mu}$ , vs lepton pair longitudinal momentum  $P_Z^{\mu\mu}$   
for **BP1 scenario** and **SM background** at 380 GeV

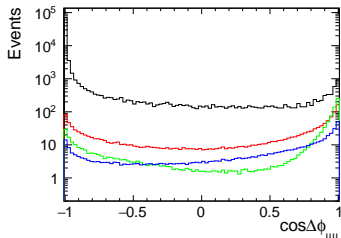
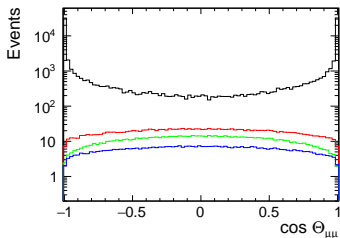
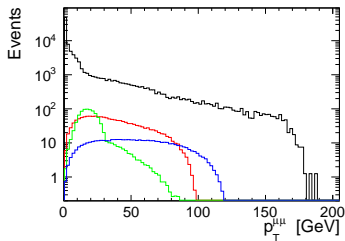
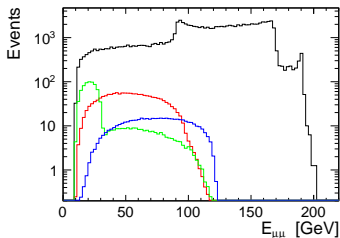


Background dominated by muon pair production ( $e^+e^- \rightarrow \mu^+\mu^-$ ) at nominal energy and radiative events ( $e^+e^- \rightarrow \mu^+\mu^-\gamma$ )

⇒ apply pre-selection cuts:  $M_{\mu\mu} < 100$  GeV and  $|P_Z^{\mu\mu}| < 140$  GeV

# Neutral scalar production @ 380 GeV ( $500 \text{ fb}^{-1}$ )

Distributions of the kinematic var. describing the leptonic final state

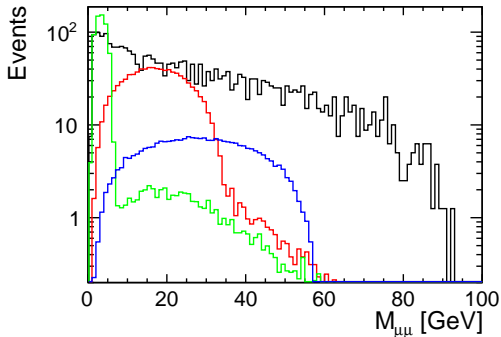


— SM — BP1 — BP2 — BP7

## Cut based approach

Lepton pair invariant mass distribution after selection cuts:

- pair energy  
 $E_{\mu\mu} < 100 \text{ GeV}$
- transverse momentum  
 $p_T^{\mu\mu} > 10 \text{ GeV}$
- production angle  
 $30^\circ < \Theta_{\mu\mu} < 150^\circ$
- azimuthal distance  
 $|\Delta\varphi_{\mu\mu}| < \frac{\pi}{2}$



Considered IDM scenarios result in the visible event excess  $15\sigma$ ,  $11\sigma$  and  $5\sigma$ , for **BP1**, **BP2** and **BP7**

## Multivariate analysis

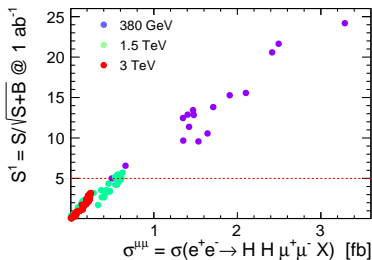
- aim: best possible discrimination between Background and Signal  
( $\Rightarrow$  highest significance)
  - Boosted Decision Tree classification algorithm in TMVA toolkit
  - BDT classifier with 8 input variables used for selection of signal events
  - not all independent (system described by 5 param.)
  - better significance if we use all 8:
- total energy of the muon pair,  $E_{ll}$
  - dilepton invariant mass,  $M_{ll}$
  - dilepton transverse momentum,  $p_{T}^{ll}$
  - polar angle of the dilepton pair,  $\Theta_{ll}$
  - Lorentz boost of the dilepton pair,  $\beta_{ll} = p_{T}^{ll}/E_{ll}$
  - $\ell^{-}$  production angle with respect to the beam direction, calculated in the dilepton center-of-mass frame,  $\Theta_{\ell}^*$
  - $\ell^{-}$  production angle with respect to the dilepton pair momentum direction, calculated in the dilepton center-of-mass frame,  $\angle^*(\ell, \ell\ell)$
  - reconstructed missing (recoil) mass  $M_{\text{miss}}$  (calculated assuming nominal  $e^{+}e^{-}$  collision energy)



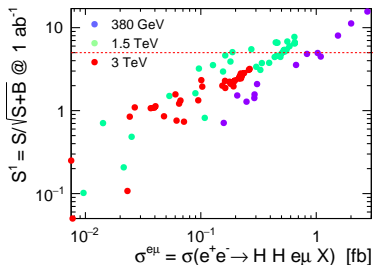
## Significance vs cross-section

Significance scaled to the same integrated luminosity of  $1000 \text{ fb}^{-1}$  as a function of the signal channel cross section

$AH$  signature ( $\mu^+\mu^-$ )



$H^+H^-$  signature ( $\mu^\pm e^\mp$ )



Expected significance mainly related to the signal channel cross section!  
 $\sim 0.5 \text{ fb}$  sufficient for the discovery...