

System:

CVD graphene grown on top of SiC
**Al electrodes in a
Superconductor/ Graphene /Superconductor**
coplanar **Josephson Junction** structure

Arturo Tagliacozzo

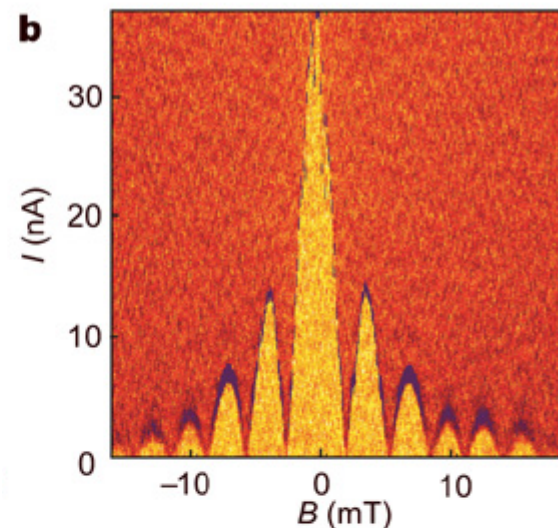
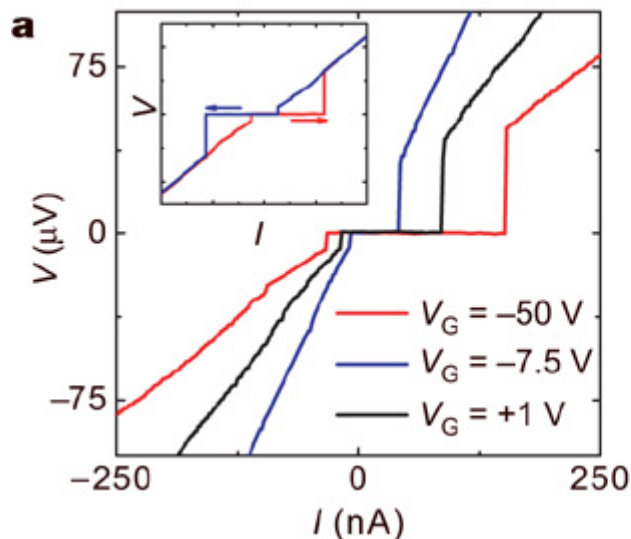
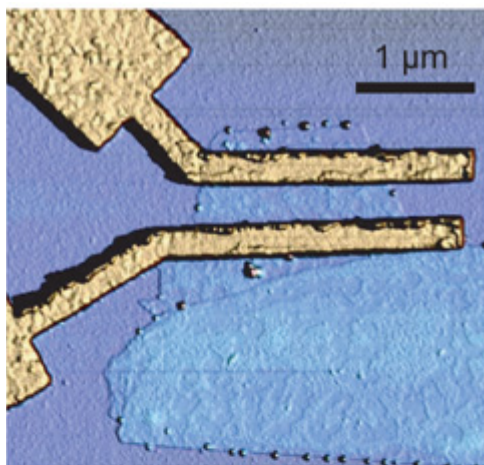
*Universita' di Napoli « Federico II »,
Napoli (Italy)*

Natal, March 27,2017

D. Massarotti, B. Jouault, V. Rouco, S. Charpentier, T. Bauch, A. Michon, A. De Candia,
P. Lucignano, F. Lombardi, F. Tafuri, and A. Tagliacozzo, Phys. Rev. B 94, 054525 (2016)
B. Jouault, S. Charpentier, D. Massarotti, A. Michon, M. Paillet, J.-R. Huntzinger, A. Tiberj, A.-A. Zahab,
T. Bauch, P. Lucignano, A. Tagliacozzo, F. Lombardi, F. Tafuri, Journal Superconductivity and Novel Magnetism 29,1145 (2016)
D. Massarotti, B. Jouault, V. Rouco, G. Campagnano, D. Giuliano, P. Lucignano, D. Stornaiuolo, G. P. Pepe,
F. Lombardi, F. Tafuri, A. Tagliacozzo, J Supercond Nov Magn 30, 5 (2017).

Graphene Josephson Junctions (GJJ)

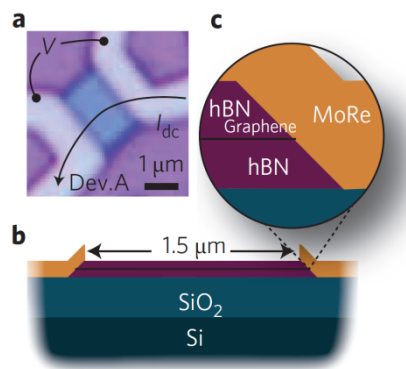
first GJJ exfoliated graphene on SiO₂... H. B. Heersche *et al.*, Nature **446**, 56 (2007)



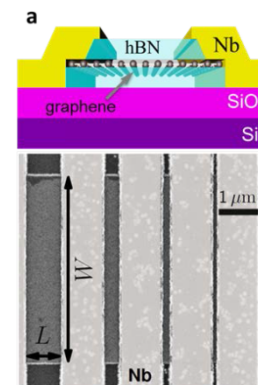
Lots of experimental efforts devoted to the realization of ballistic devices,



N. Mizuno *et al.*, Nature Comm. **4**, 2716 (2013)



V. E. Calado *et al.*, Nature Nano **10**, 761 (2015)



M. Ben Shalom *et al.*, Nature Physics **12** (4), 318 (2016)

CVD graphene on SiC

Limit of exfoliated graphene:

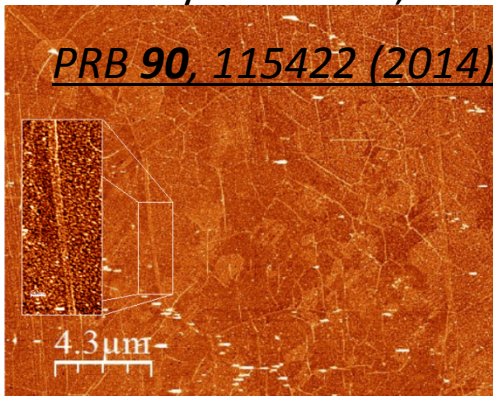
- Small devices only (no SQUID, no Voltage Standards...),
- geometry hard to control/reproduce

Solution? CVD graphene

Very large surface = reproducibility and scalability
many junctions built on the same graphene/same lithography:
electrodynamics can be studied without ambiguity

CVD graphene on metals

Pros: any substrate, *Cons:* transfer!



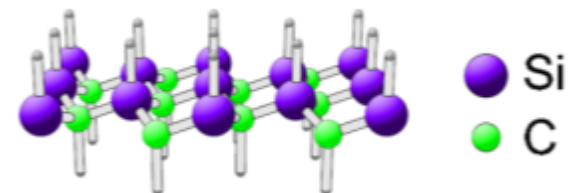
CVD graphene on SiO_x

Tianyi Li *et al*, *arXiv 1703.06049*

(CVD, sublimated) graphene on SiC

Pros: No transfer

Cons: substrate is SiC! (low mobility)



This is the way we study here

Incipient Berezinskii Kosterlitz and Thouless transition in 2D coplanar Al contacted graphene junctions

Arturo Tagliacozzo

Universita' di Napoli « Federico II », Napoli and CNR , Italy



D. Massarotti, V. Rouco, A. De Candia,
P. Lucignano, F. Tafuri

CNR, SUN, Naples, Italy

Benoît Jouault

*Lab Charles Coulomb, CNRS, Montpellier,
France*

S. Charpentier, T. Bauch, F. Lombardi
Chalmers, Sweden

M. Paillet, J.-R. Huntzinger, A. Tiberj, A. Zahab
L2C, France

A. Michon

CRHEA, Valbonne, France

Natal, March 27, 2017

Outline

Prerequisites

- 1) Graphene on SiC: characterization
- 2) Lithography

First results

- 1) $V(I)$ curves, Josephson critical current, $I_c R_N$ product

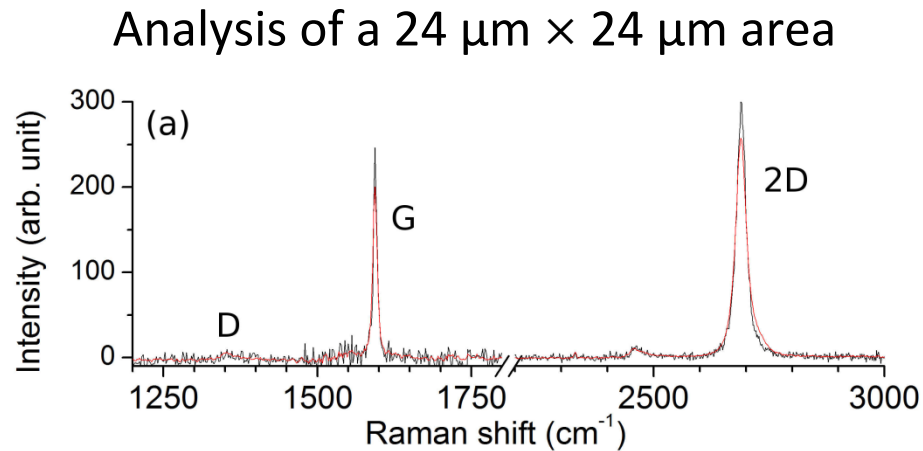
Applied Magnetic field

- 1) magnetic field fingerprint
- 2) Collapse and revival of the Josephson current
- 3) Fraunhofer pattern

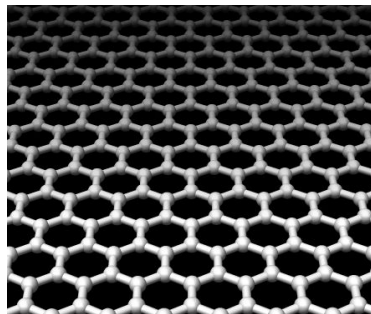
R(T): fit with Berezinskii-Kosterlitz-Thouless theory for thin films

***Proposed interpretation:* incipient BKT transition in form of
coexistence of flux flow superconductivity with
Josephson current**

CRHEA sample, Raman analysis

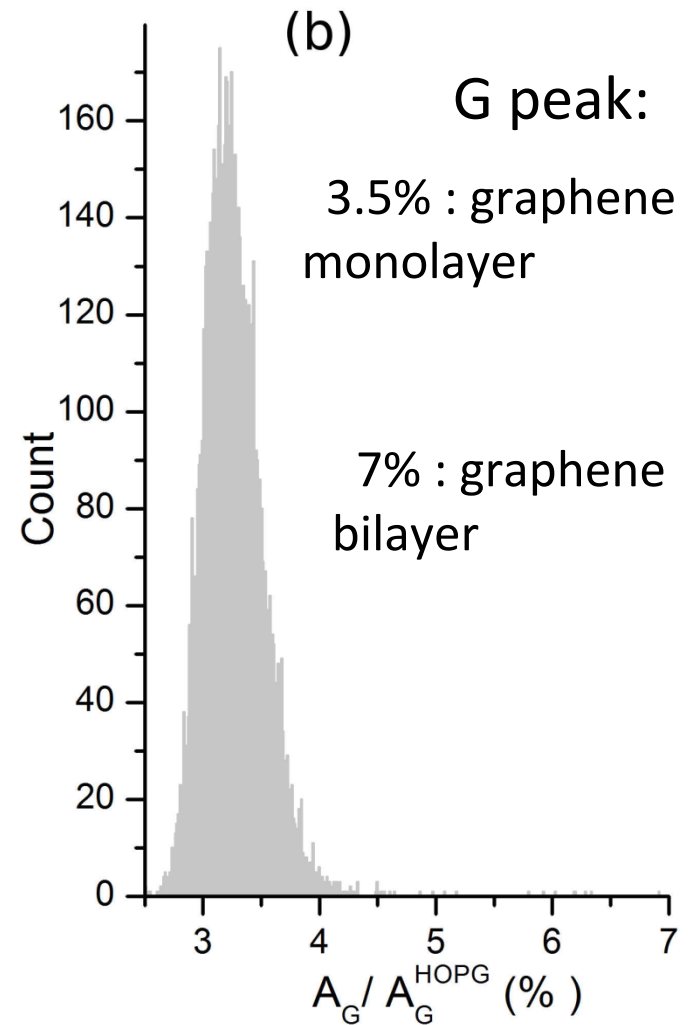


Small D peak: few defects



$\mu \sim 1,100 \text{ cm}^2/\text{Vs}$

low mobility

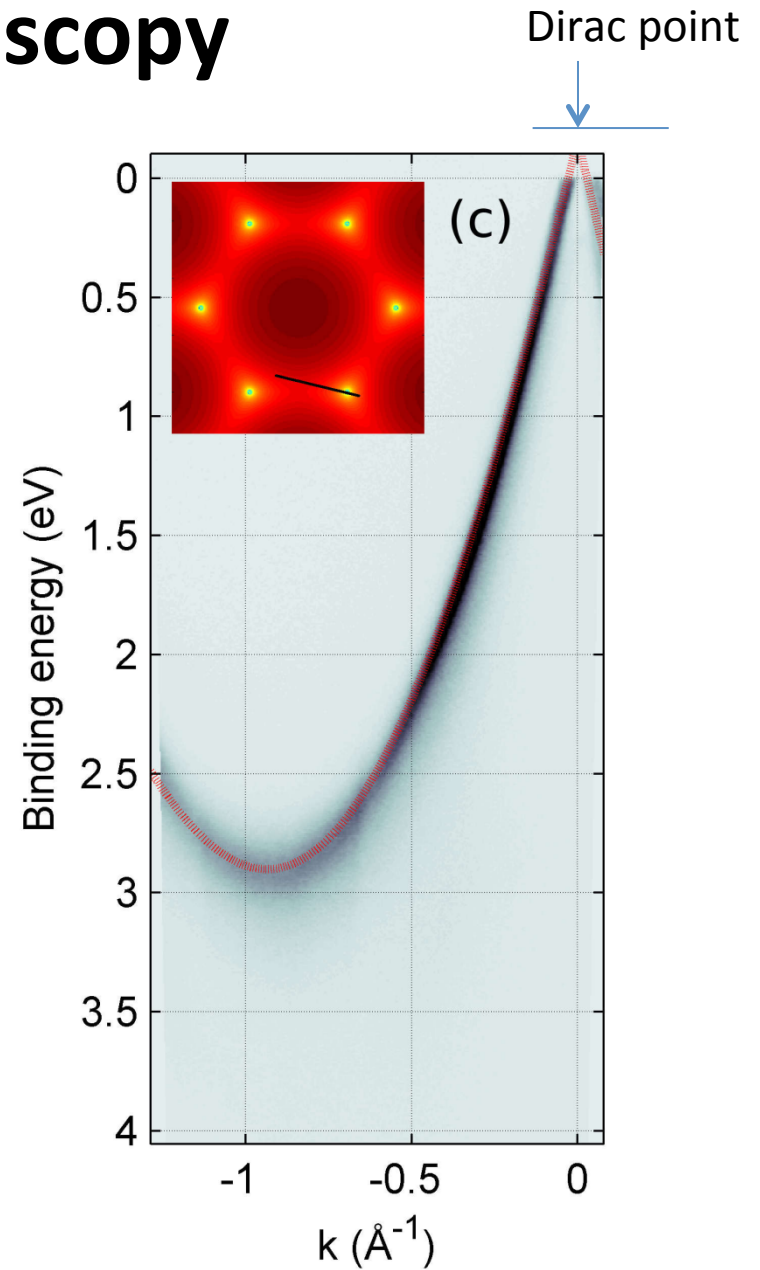
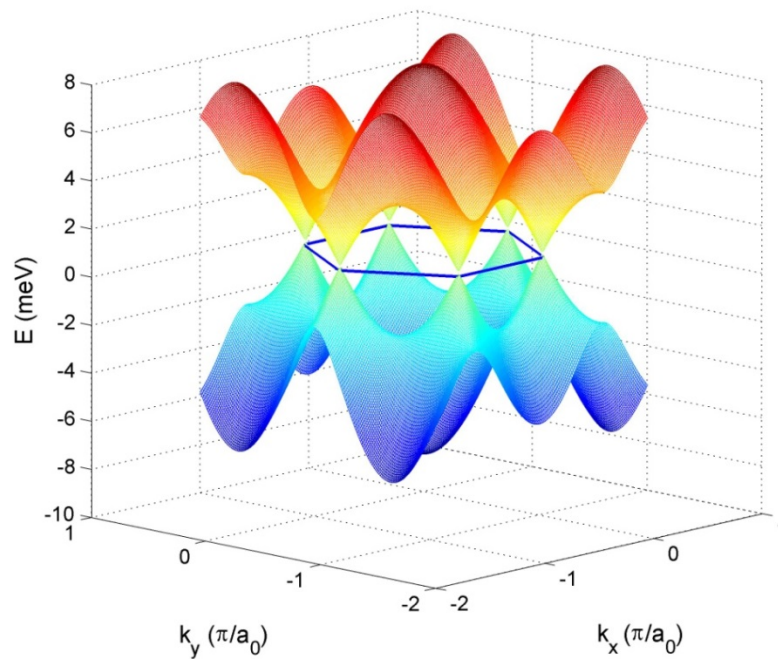


This sample is a homogeneous graphene monolayer

ARPES Spectroscopy

Monolayer graphene, p-doped,
 $p \approx 5 \times 10^{12} \text{ cm}^{-2}$

Perfect fit (red line) with the predicted
graphene band structure:



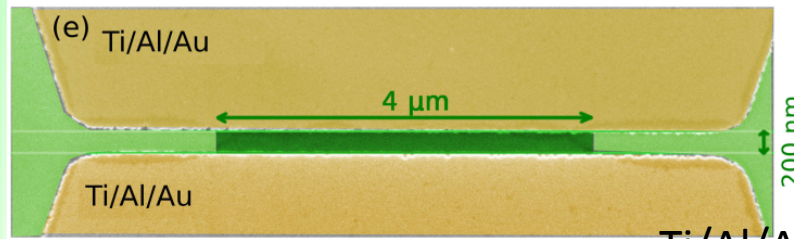
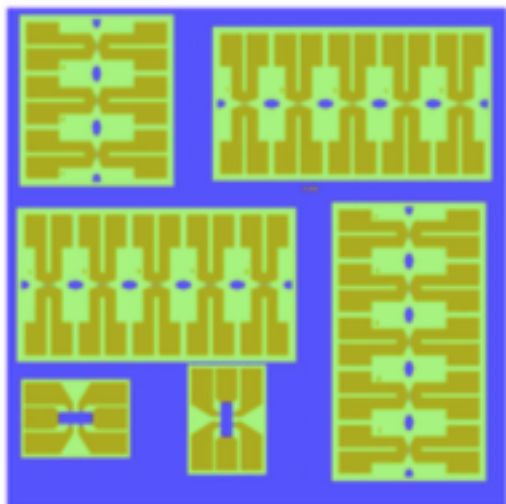
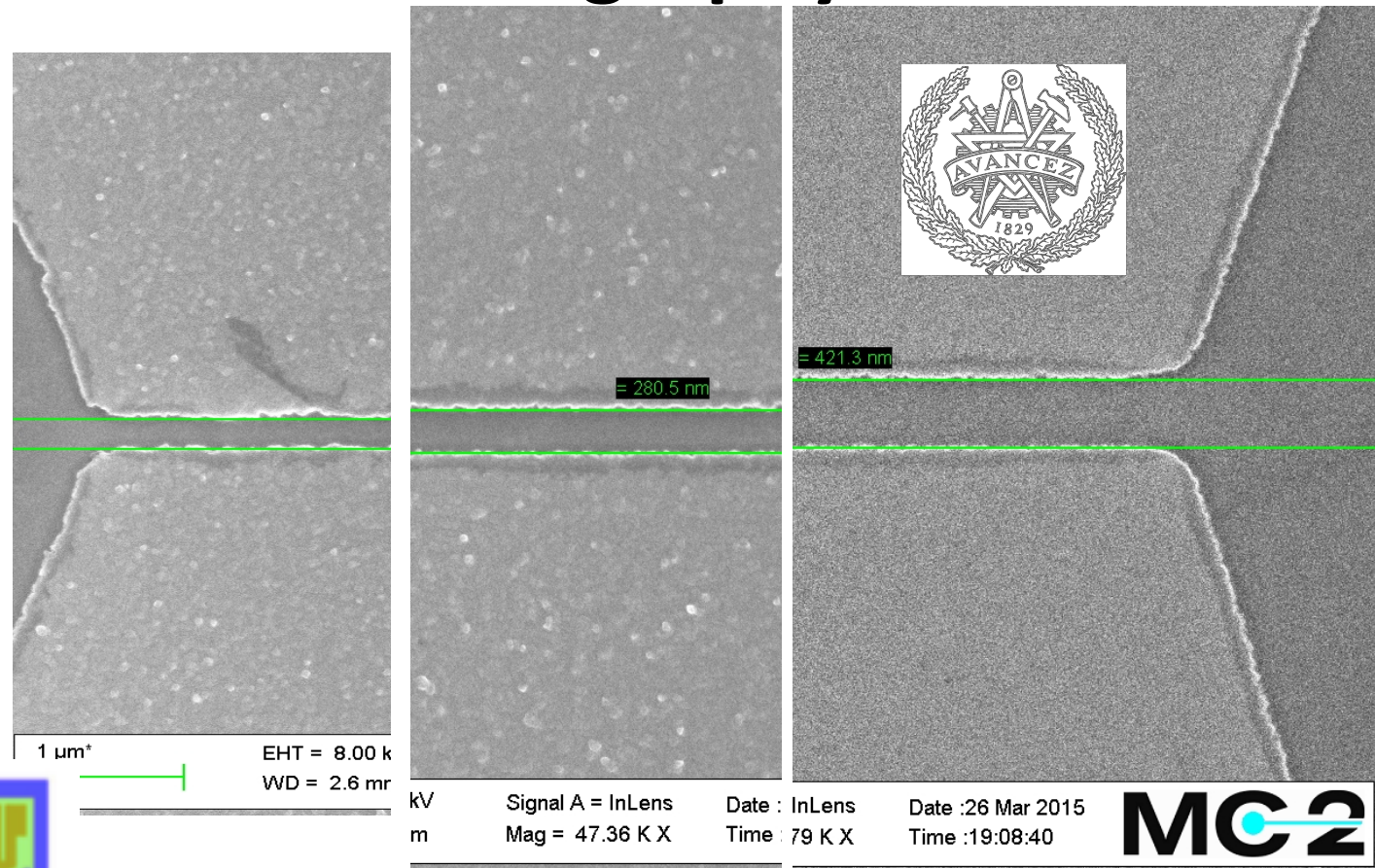
A. H. Castro-Neto *et al.*, RMP **81**, 101 (2009)

E-beam lithography

No gate at this stage
 $\mu \sim 1,100 \text{ cm}^2/\text{Vs}$

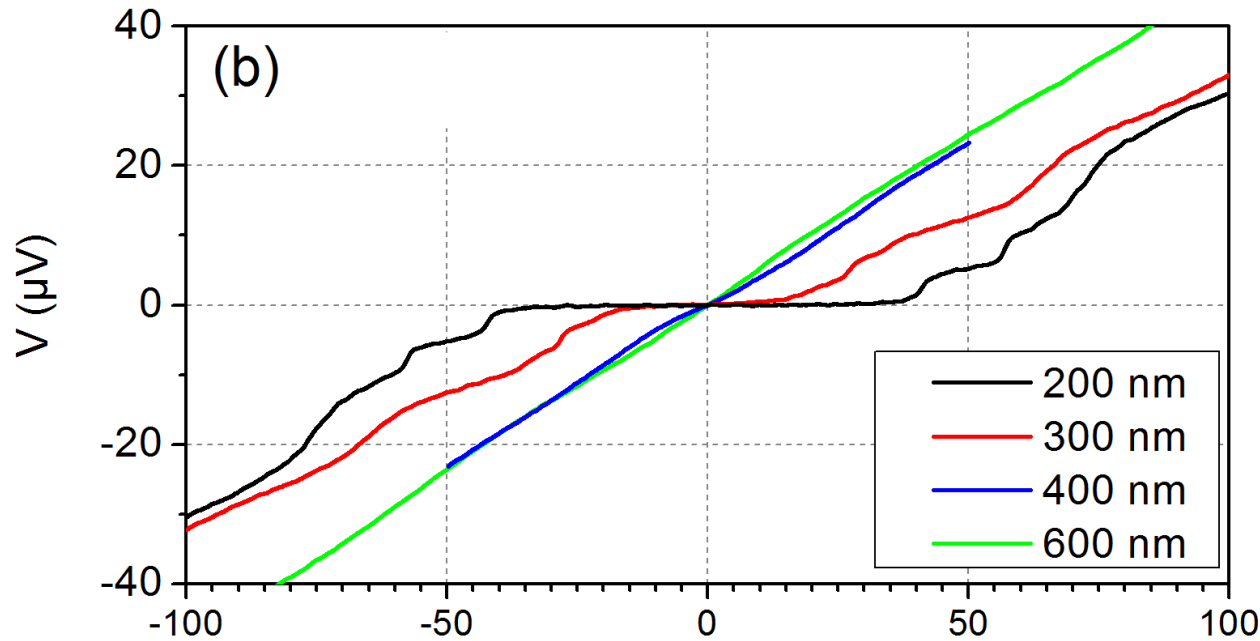
O₂ plasma etching

Many junctions on the same graphene sheet

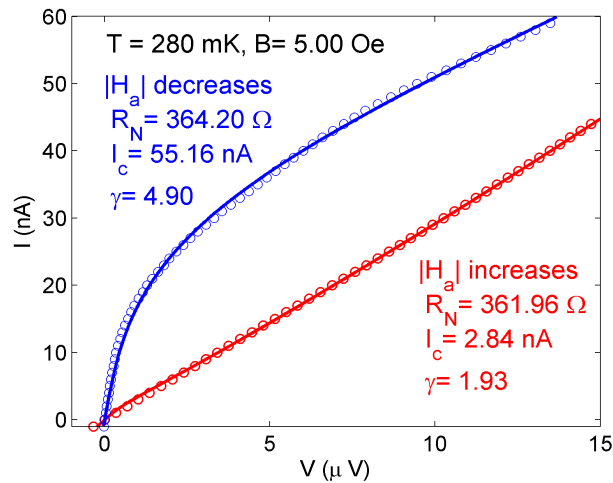


Ti/Al/Au contacts
 5/80/3 (nm)

V(I) curves at 280 mK



RSJ
classical
model



$\ell \sim 50 \text{ nm}$: all junctions **diffusive**.

Al gap $\Delta \sim 100 \mu\text{eV}$, coherence length $\xi_0 \sim$

300 nm:

Expected and observed crossover
between short and long junction limits at
 $L \sim \xi_0 \sim 300 \text{ nm}$.

$L \approx 200 \text{ nm}$, $W \approx 4 \mu\text{m}$

Our $R_N \approx 400 \Omega$

$$\frac{eI_c R_N}{\Delta} \sim 0.09 < 0.66$$

$eI_c R_N / \Delta \sim 0.09$, smaller than its theoretical estimate 0.66 :
either bad contacts or underestimation of I_c
(as $T \sim 0.3 T_c$ for Al only), but

$J_c = I_c / W \sim 10 \text{ nA } \mu\text{m}^{-1}$ at $L = 200 \text{ nm}$: in the literature, J_c
between 1 and 100 $\text{nA } \mu\text{m}^{-1}$

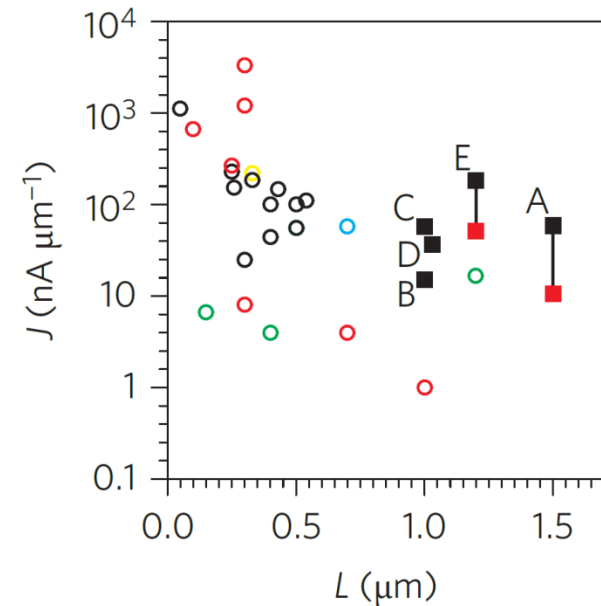
$$L \leq \xi_0 = \sqrt{\frac{\hbar D}{\Delta}} \sim 300 \text{ nm}$$



$$E_{Th} = \frac{\hbar D}{L^2} \sim \Delta$$

At the Dirac point

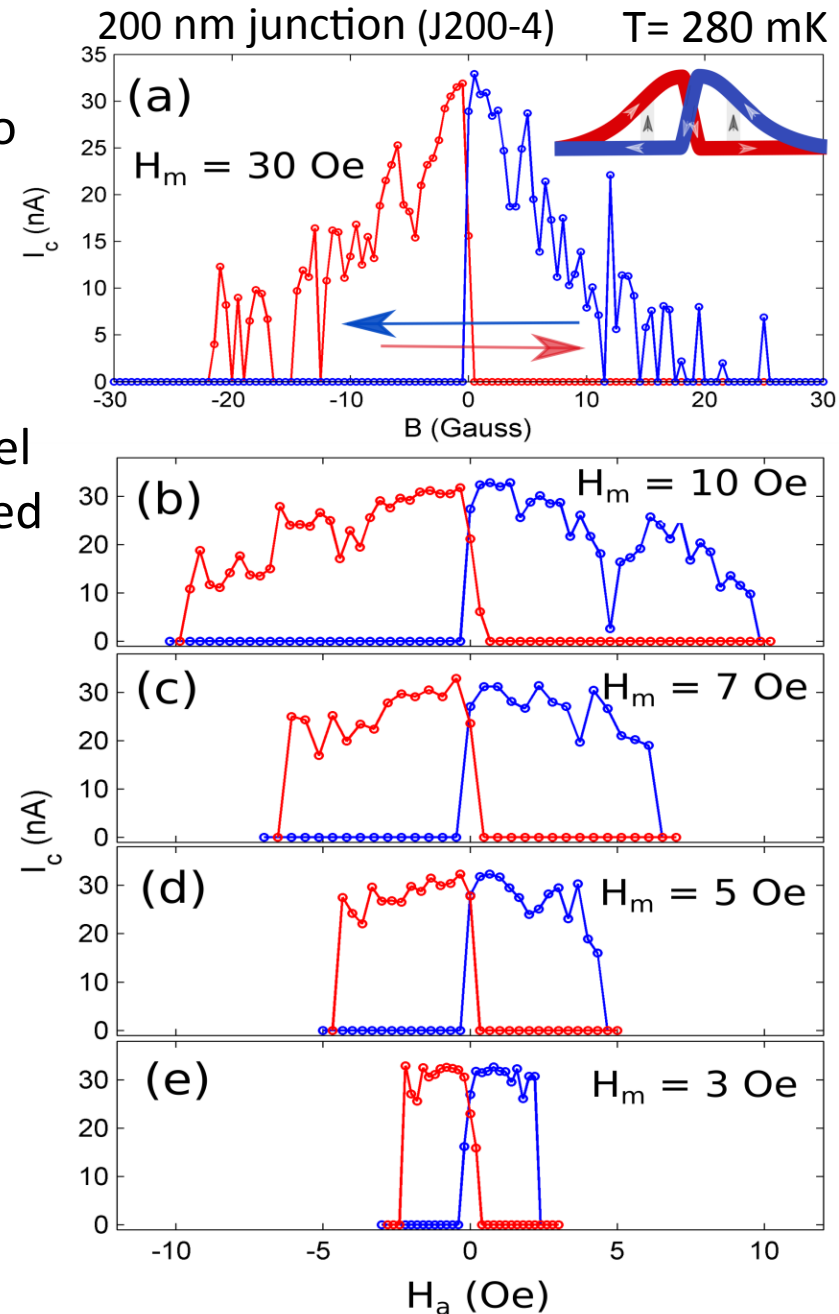
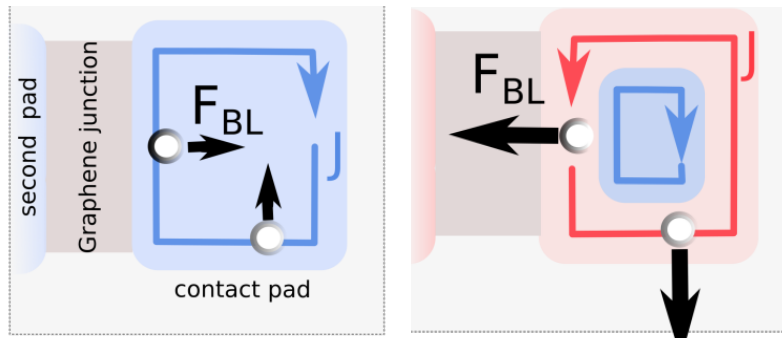
$$R_N \sim \frac{h}{e^2} \frac{L}{W} \approx 920 \Omega$$



Magnetic field hysteresis

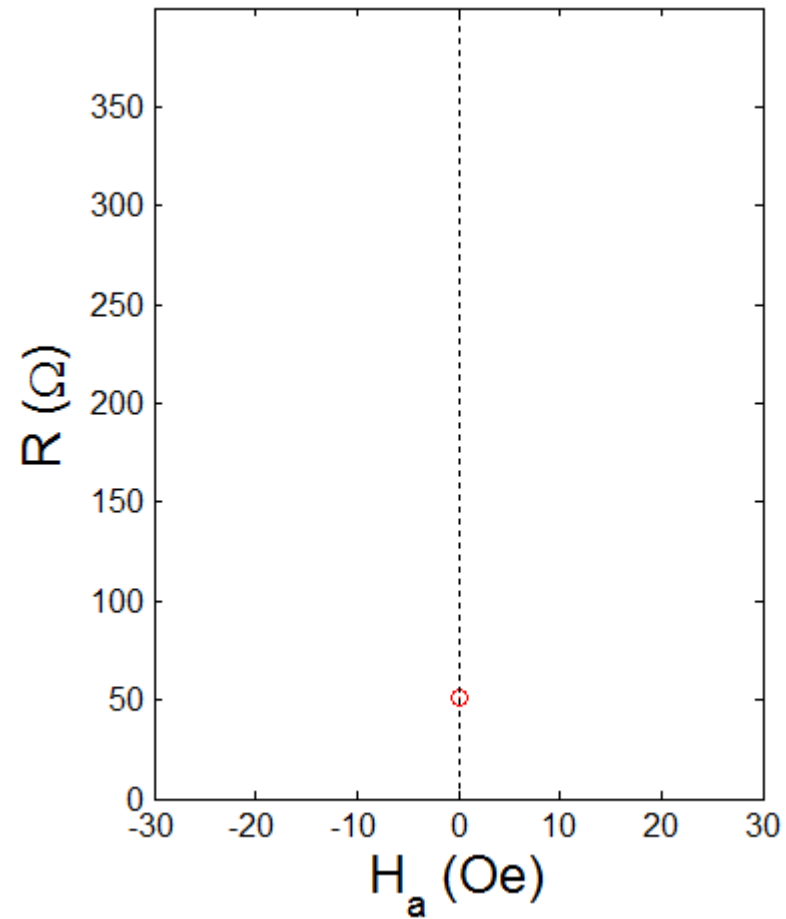
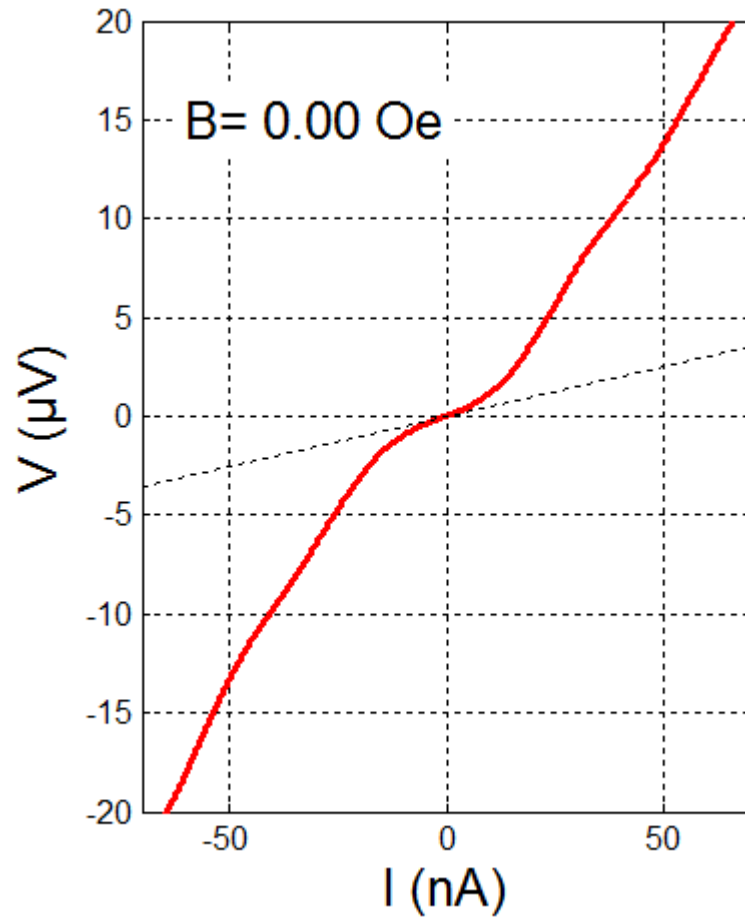
- Magnetic field hysteresis persists up to 30 Oe
- Observed on all measured junctions
- should not be so large in 2L-CSM model
- anomalous $M(B)$ curves often attributed to Bean-Livingstone (BL) barrier

BL barrier= sum of image and screening forces



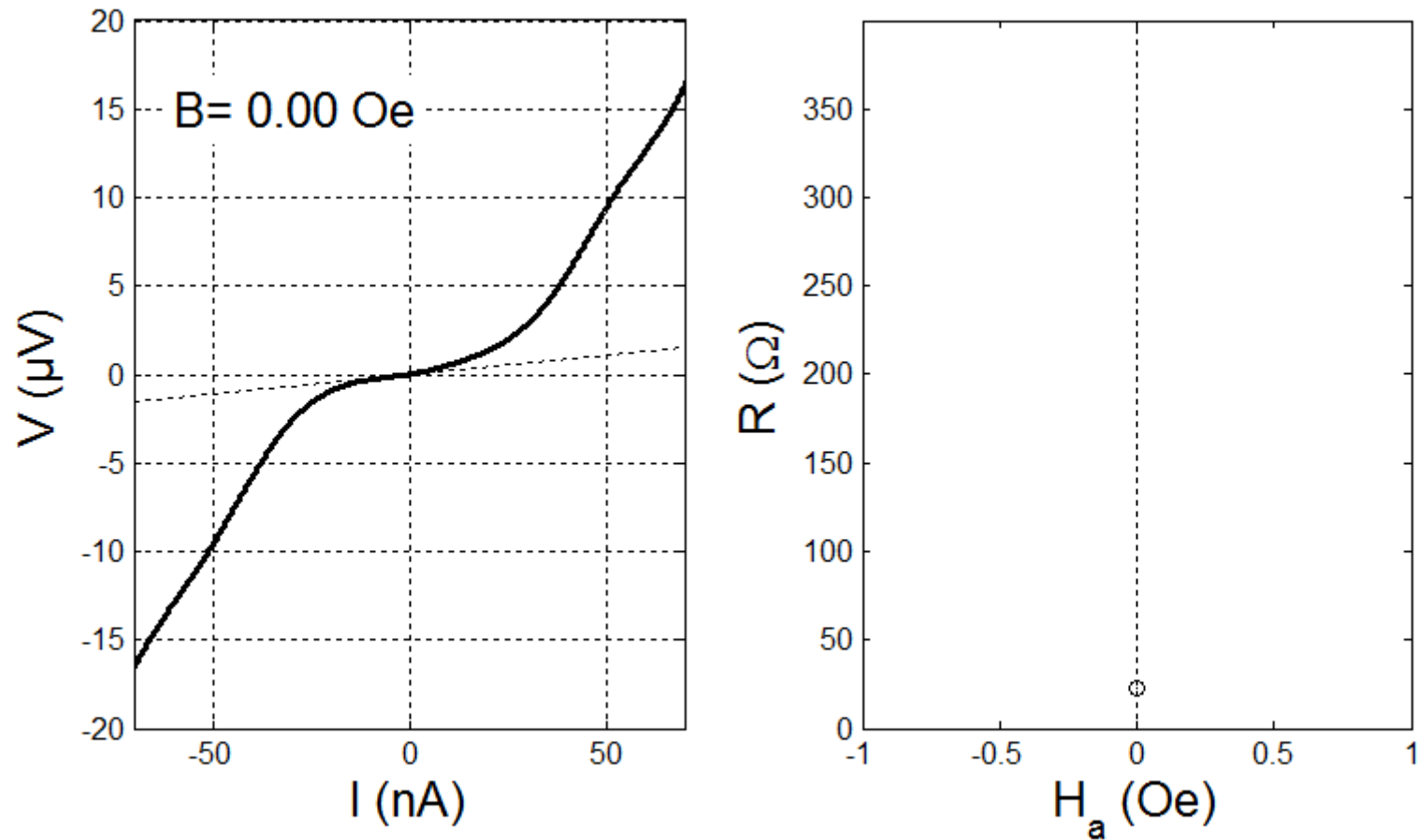
Magnetic field signature

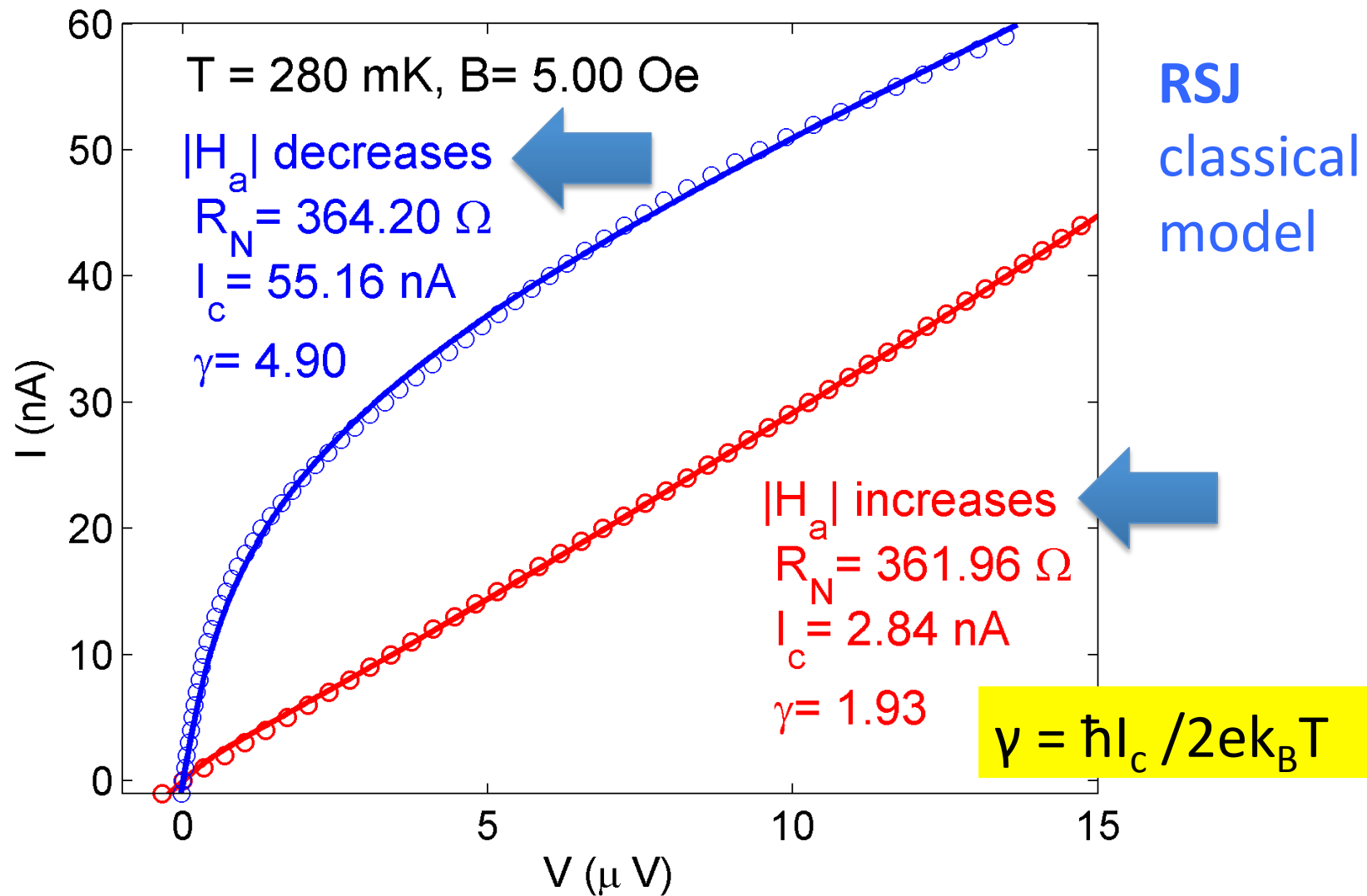
200 nm junction (J200-4) $T = 280$ mK



Magnetic field hysteresis persists up to 30 Oe

Inverted hysteresis below 1 Gauss

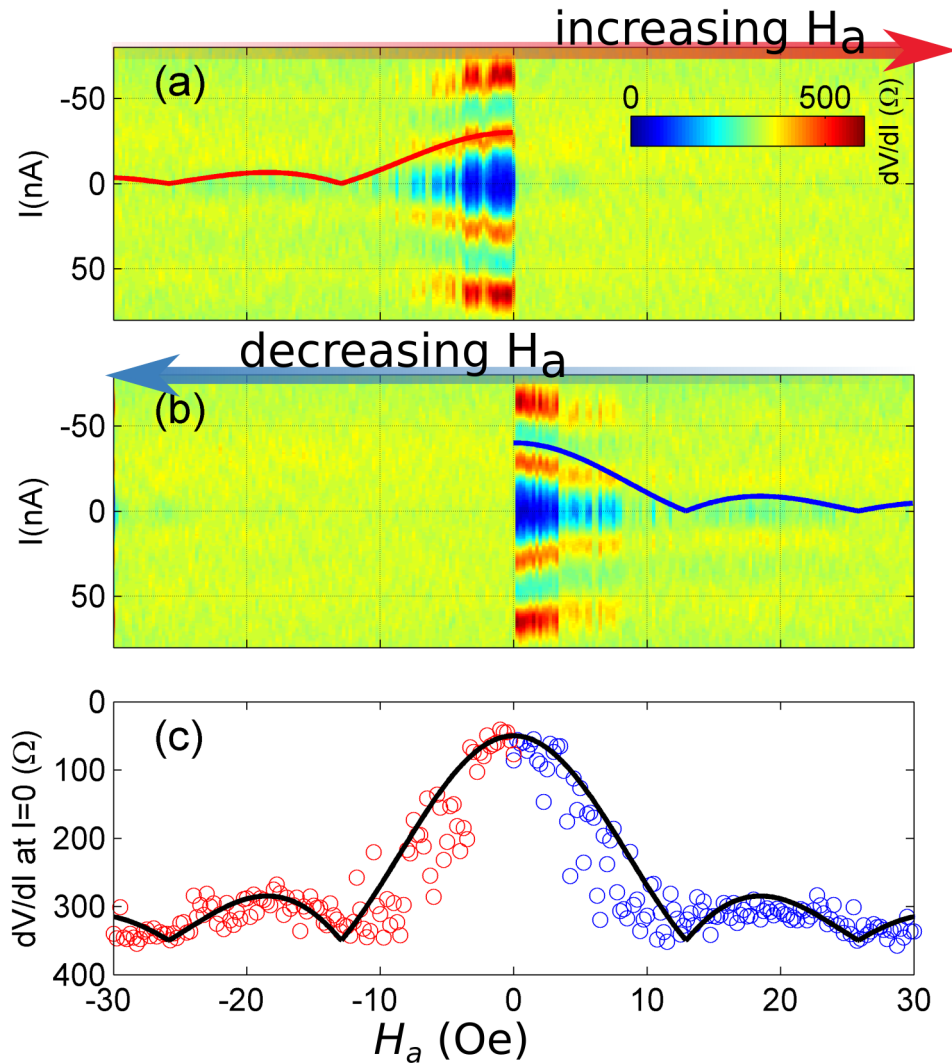




RSJ model for phase diffusion: unable to describe hysteresis

Magnetic field signature

By combining the decreasing $|H_a|$ parts (the revival)



Fraunhofer pattern (FP) retrieved

but...

FP is only the envelope of faster oscillations :

$\Delta H \sim 1-3$ Oe

effective area $S_{\text{eff}} \sim 9 \mu\text{m}^2$

nominal junction area is $WL \sim 1 \mu\text{m}^2$



Magnetic flux below and inside Al contacts

Weak screening ($\lambda > 1 \mu\text{m}$)
(typical of coplanar junctions)

first model: Rosenthal model

P. A. Rosenthal *et al.*, APL **59**, 3483 (1991):
 $\delta B \propto w^2$ in thin-film grain boundary junctions.

Assuming London penetration length $\lambda=1 \mu\text{m}$,
 we solve the London equation :

$$\nabla^2 J - \frac{1}{\lambda^2} J = 0$$

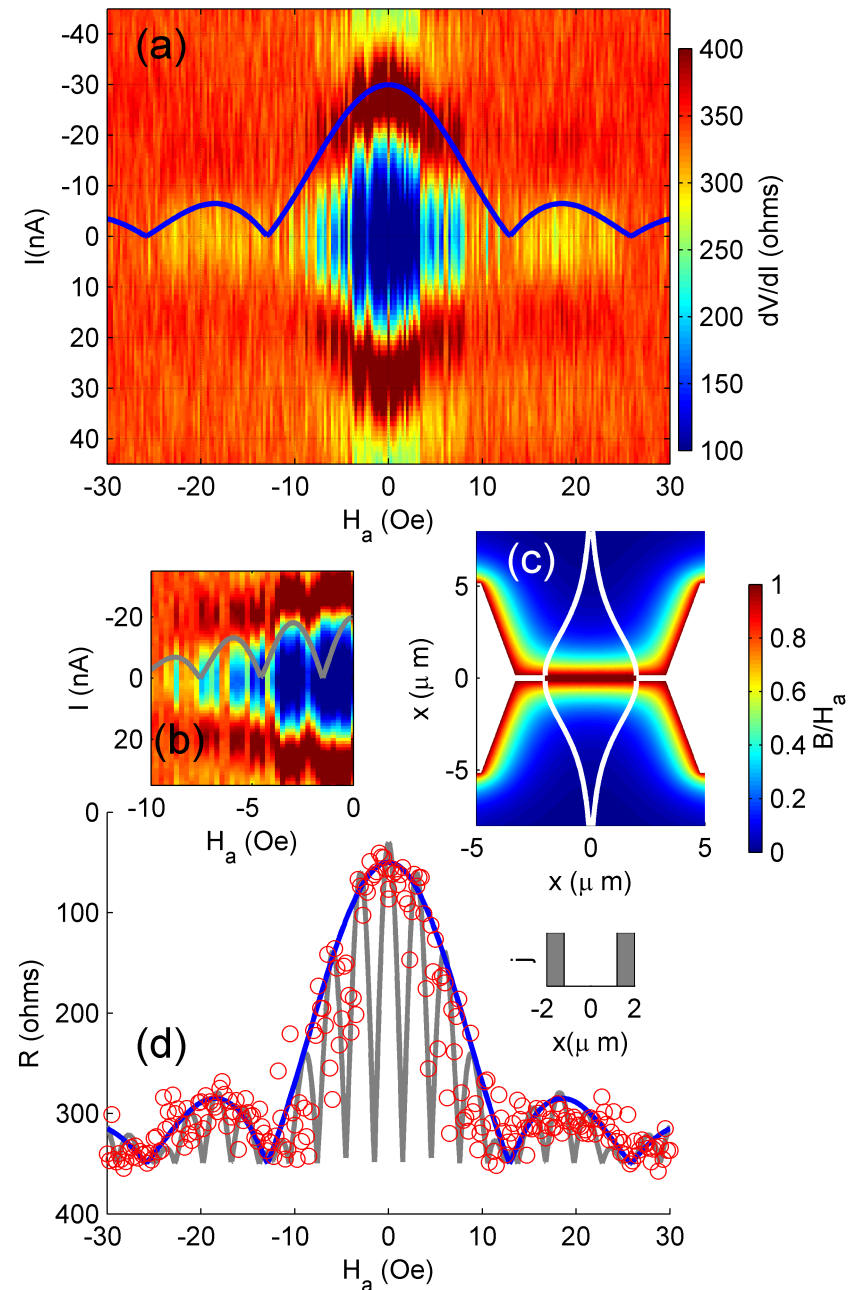
In the London Gauge:
 $\nabla \cdot \mathbf{A} = 0, \quad \mathbf{A} \cdot \mathbf{n} = 0, \quad \mathbf{A} = -\frac{\mu_0 \mathbf{J}}{\lambda^2}$

The phase can then be recalculated via:

$$\Delta\varphi = \frac{2e}{\hbar} \int \mathbf{A} \cdot d\mathbf{l}$$

- i) The fast oscillations easily reproduced
- ii) their aperiodicity is not reproduced
- iii) Fraunhofer envelope reproduced only by introducing additional inhomogeneous current distribution in the graphene junction.

...The model is not the full story but it signals the presence of flux entering and exiting the contacts



Inverted hysteresis

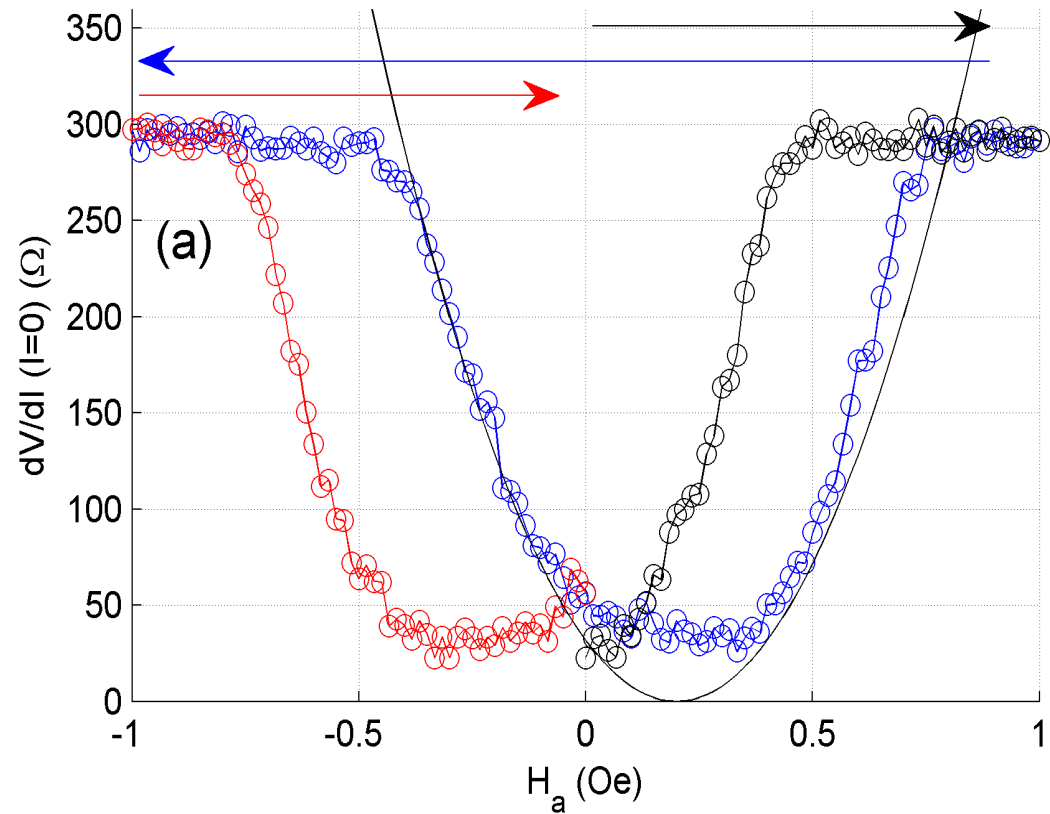
typical of type-II granular superconductor

hysteretic

inverted hysteresis
with 2 anomalous features:

when $|H|$ increases
>
when $|H_a|$ decreases

has a minimum
at 0.3 Oe
before $|H_a|$ reaches 0



below 1 Gauss

signature of flux trapping

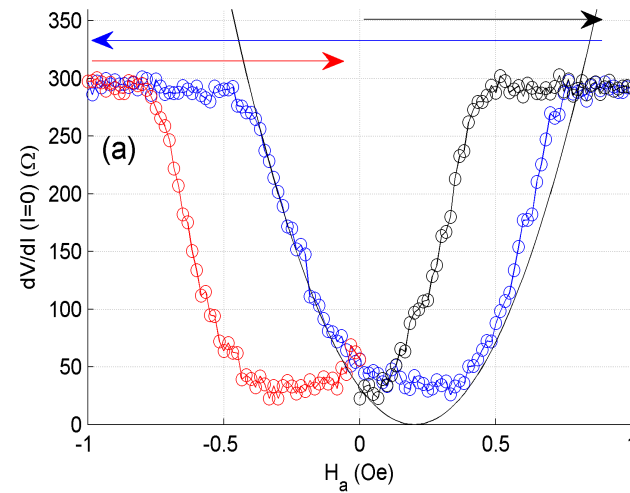
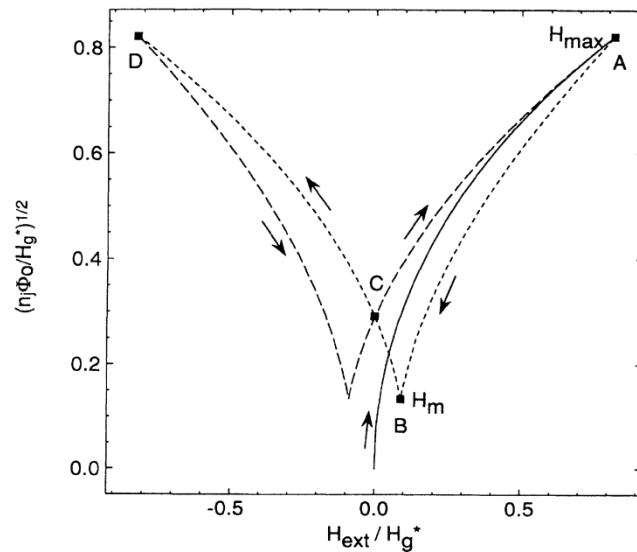
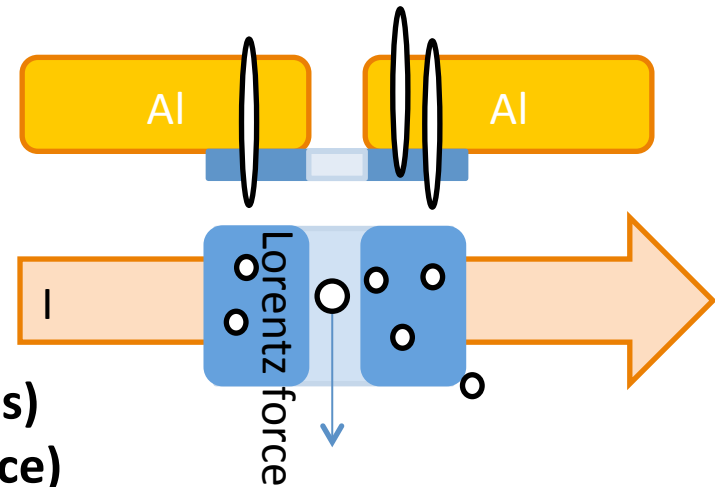
Two-level critical state model vortices

L. Ji *et al.*, PRB **47**, 470 (1993)

explain the anomalous hysteresis of granular superconductors

Implies the existence of

- 1) Grain-pinned vortices (pinning, hysteresis)
- 2) Grain-boundary vortices (electrical resistance)



Next question: what about the (bounded) parabolic shape ?

Bean-Livingstone (BL) barrier?

BL appropriate to explain asymmetric hysteresis

BL barrier to introduce or expel vortices inside the type II superconductor

(a) increasing $|H_a|$

image and screening forces are opposite
Vortex driving force moderate

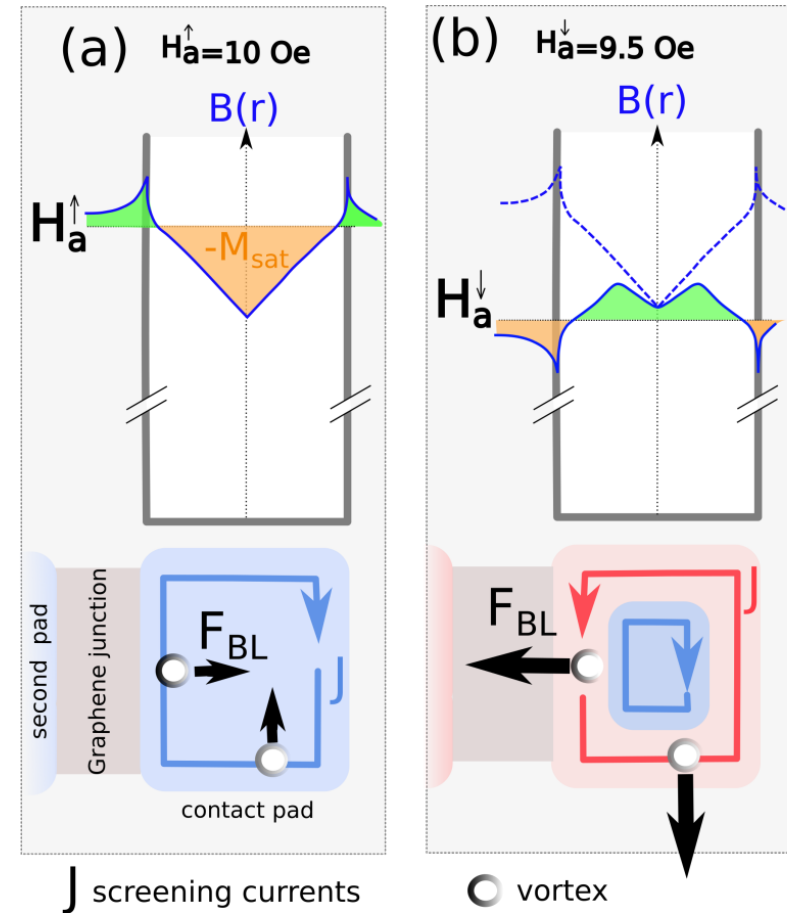
(b) decreasing $|H_a|$, screening current reversed

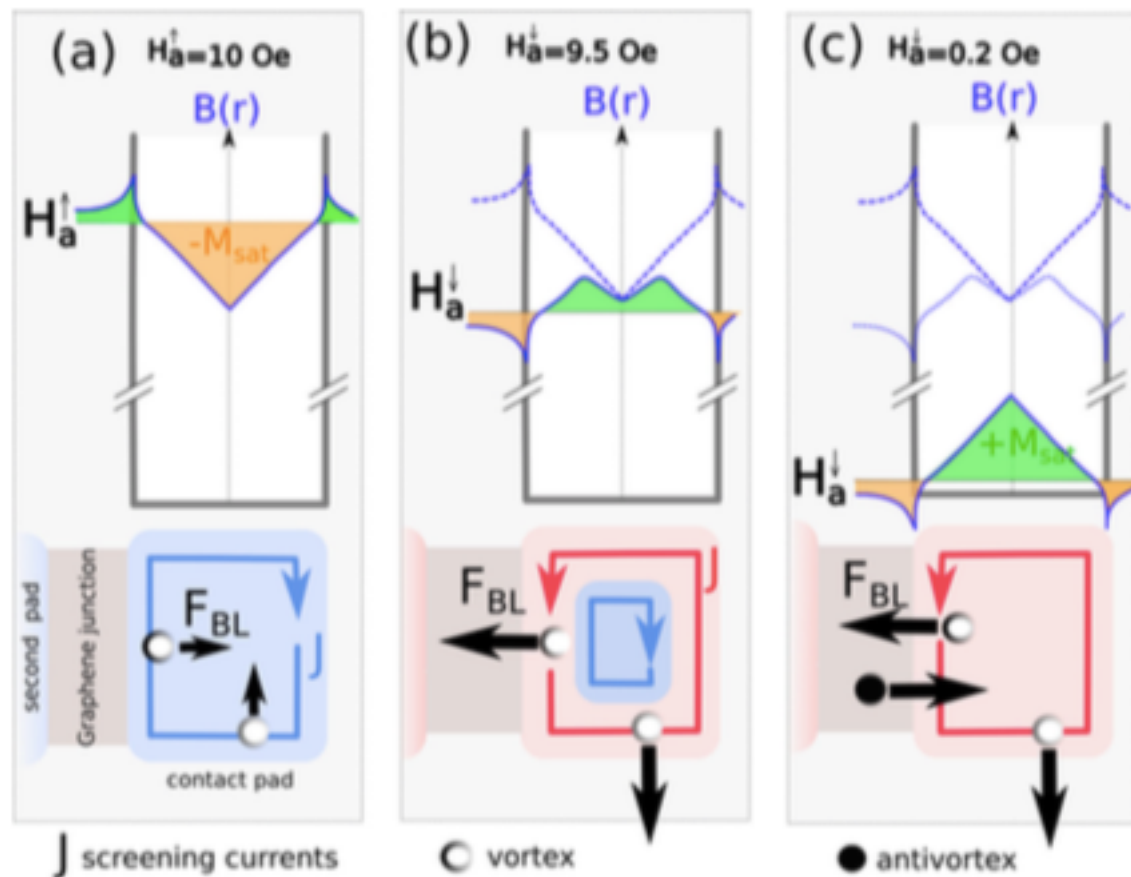
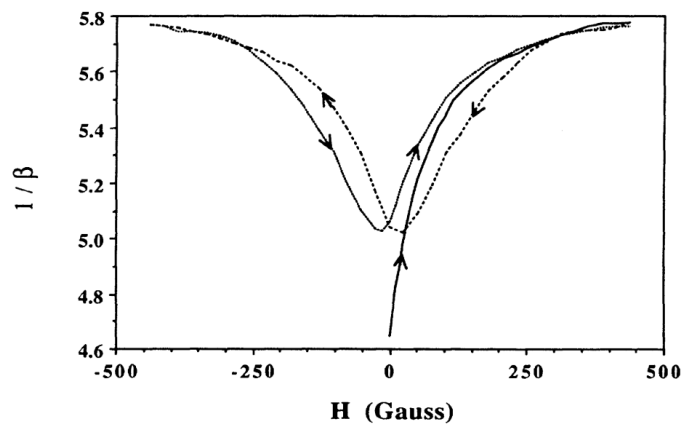
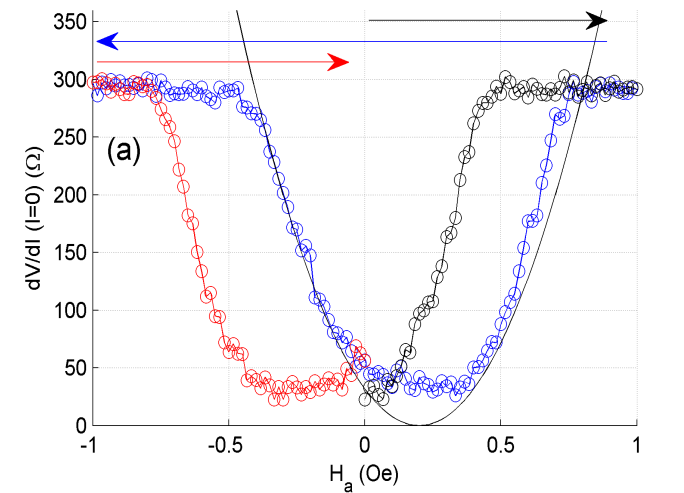
image and screening forces both
expel vortices

only strongly pinned vortices are not
expelled

In the CSM, pinning force

Dissipation possibly reduced at
the graphene junction barrier





R(H): classical simulations

$N=2048$ 2D disks

Interaction potential is

$$u(r) = (\sigma/r) + e^{-r/\lambda} / \lambda^2$$

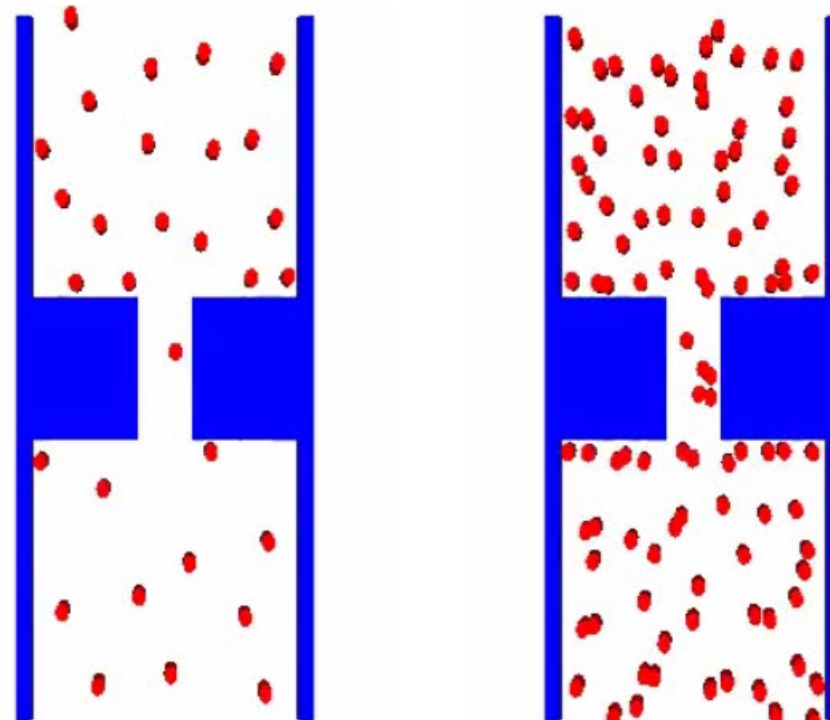
$$\sigma = 1 \mu\text{m}, \lambda = 8 \mu\text{m}$$

Vortex density = H/ϕ_0

Number of vortices $N = \rho L^2$

Viscosity $\eta =$ inverse of
diffusion coefficient D

$$R \propto E/j_{\text{ext}} \propto H\nu/\eta v \propto \rho/\eta$$



$H = 0.7 \text{ Oe}$

$H = 2.5 \text{ Oe}$

Vortex diameter = $0.5 \mu\text{m}$

R(H): classical simulations

Flux flow resistance

$$\rho_f = \frac{E}{j_{ext}} = H \frac{\phi_0}{\eta c^2}$$

N= 2048 2D disks

Interaction potential is

$$u(r) = \sigma^2/r^2 + \exp[-r^2/\lambda^2]$$

$$\sigma = 1 \mu m, \lambda = 8 \mu m$$

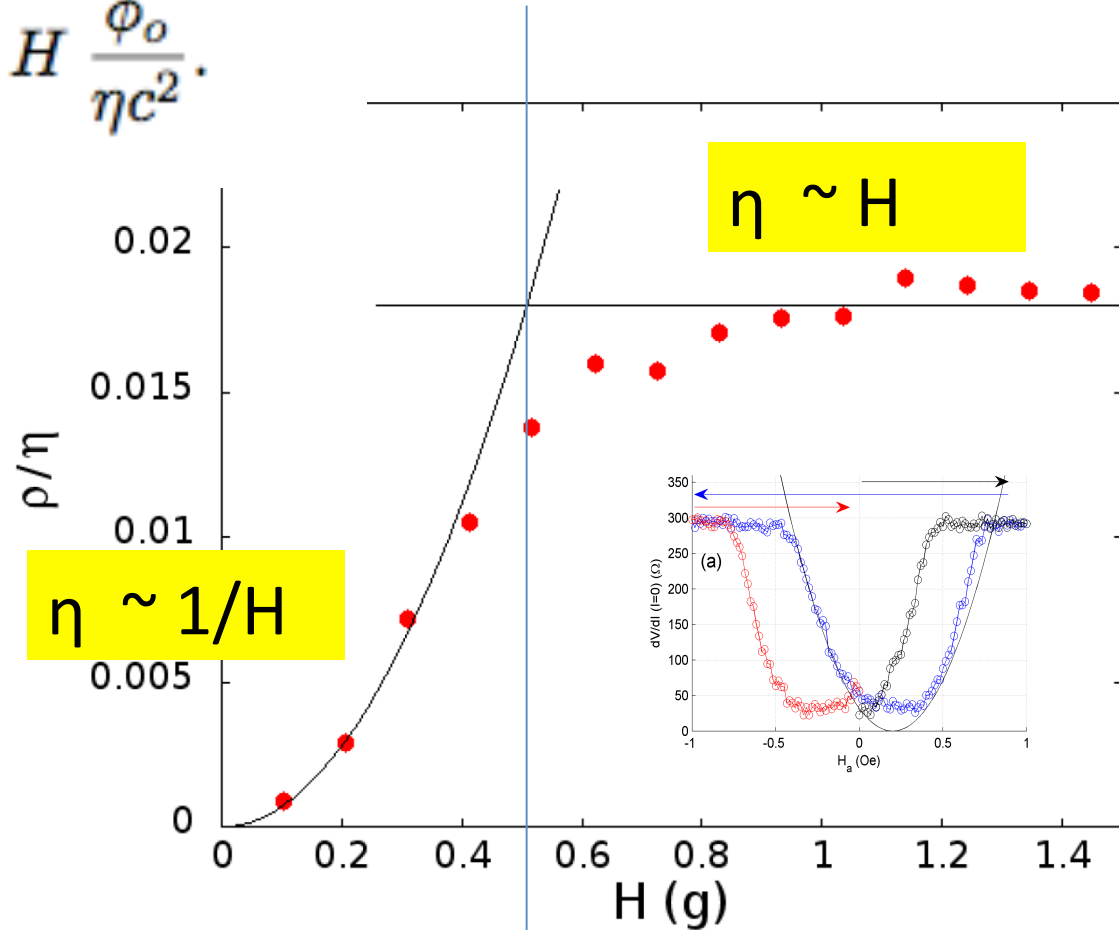
Vortex density $\rho = H / \phi_0$

Number of vortices $N = \rho L^2$

Viscosity η \sim inverse of

Diffusion coefficient D

$$R \sim E / j_{ext} \sim H v / \eta v \sim \rho / \eta$$

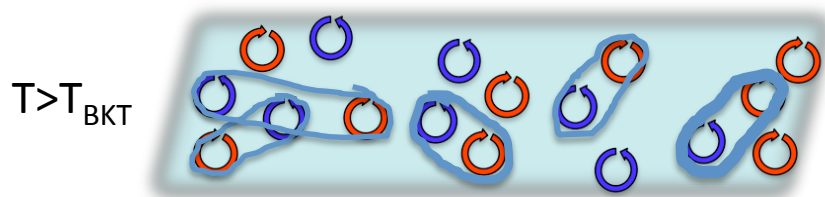


High viscosity	low viscosity
Long range interaction	short range interaction
solid	liquid

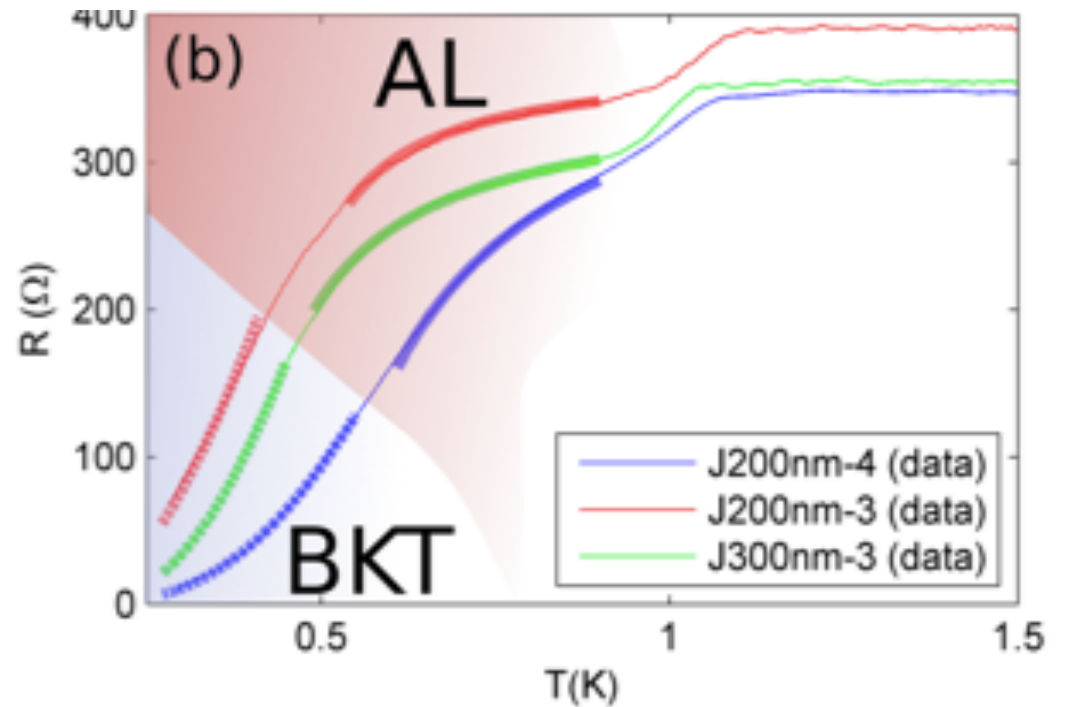
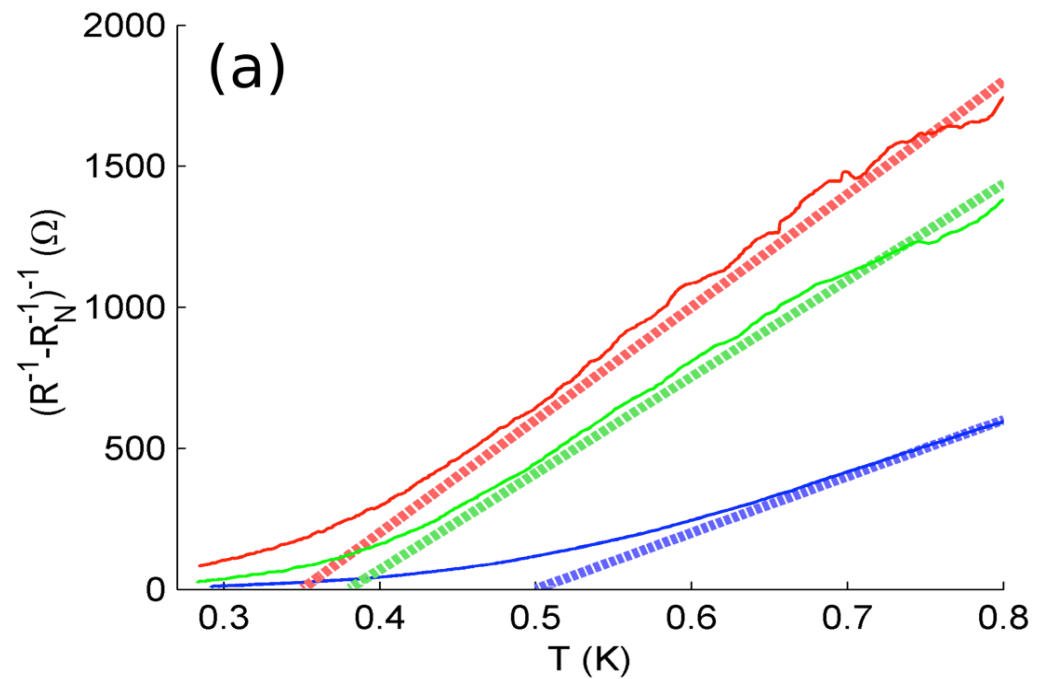
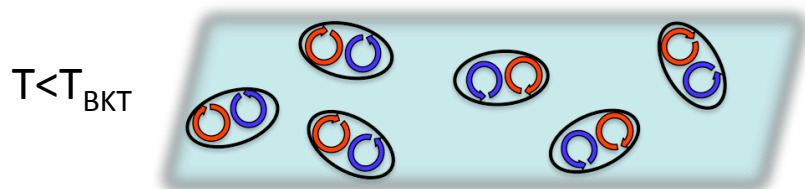
Incipient BKT transition

$T > T_{c0}$ Paraconductivity :
Aslamasov-Larkin

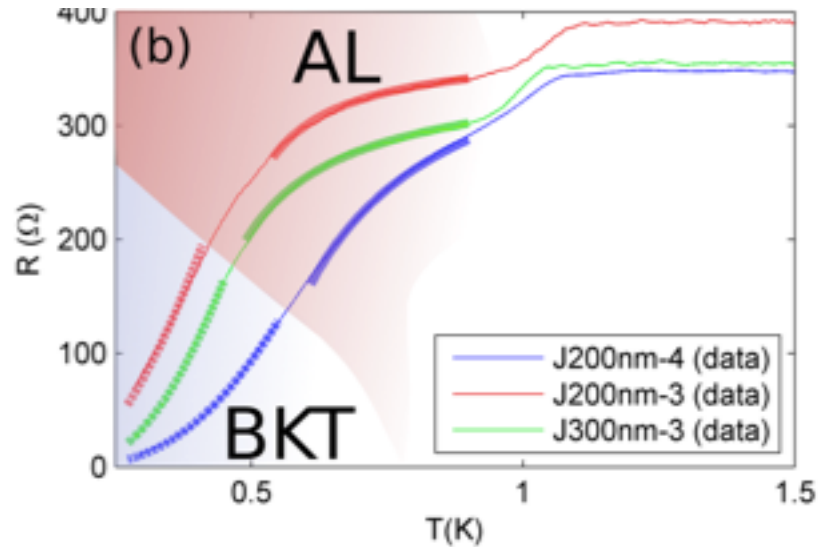
Low $T < T_{c0} = 500\text{mK}$: $R(T)$
compatible with vortex/
antivortex pair formation



$T > T_{\text{BKT}} \sim 50 \text{ mK}$: breaking of
vortex/antivortex pairs



R(T) transition

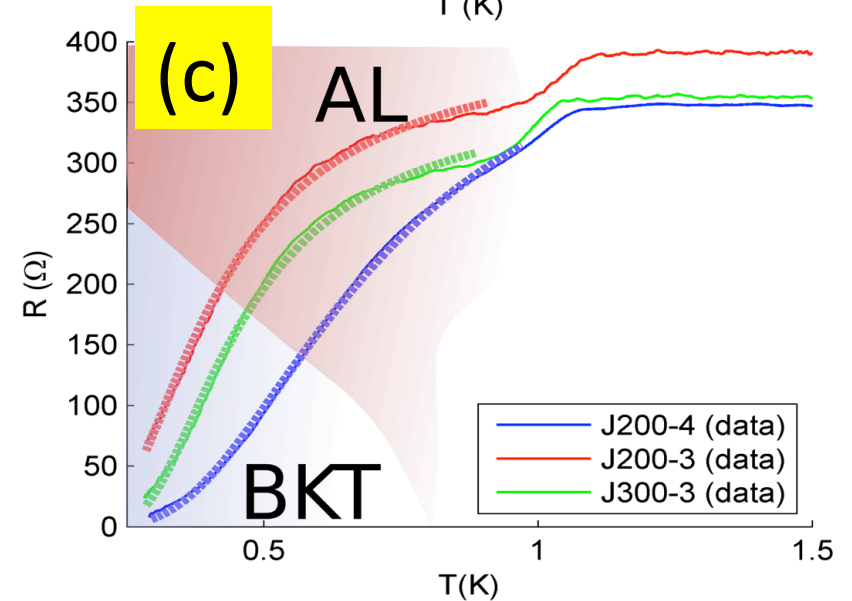
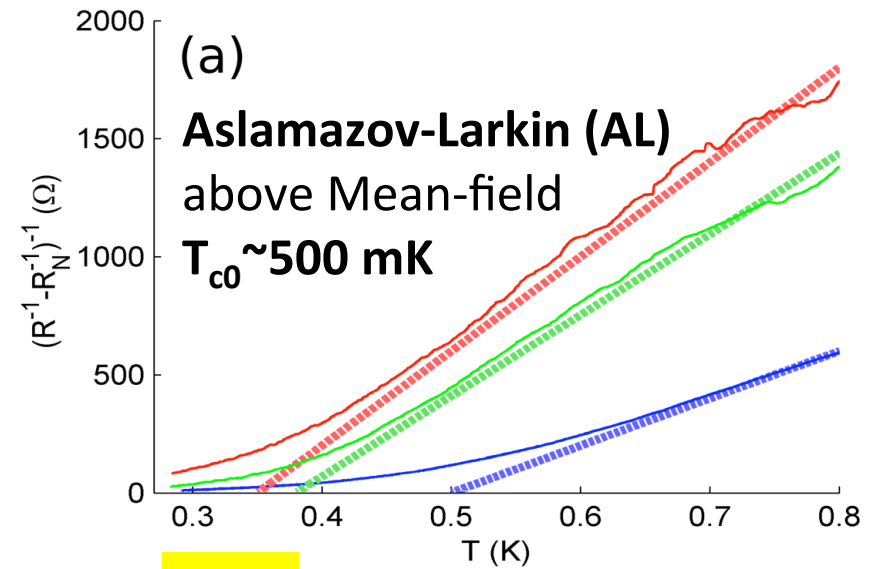


Berezinskii-Kosterlitz-Thouless (BKT) fit $50 \text{ mK} \sim T_{\text{BKT}} < T < T_{\text{c0}}$

$$R(T)^{-1} = \frac{0.37}{b} R_N^{-1} \sinh^2 \left(\frac{bt_c}{t} \right)^{1/2}$$

Halperin-Nelson crossover fit for $R(T)$ at $T_{\text{BKT}} < T$ (1979)

$$t = (T - T_{\text{BKT}}) / T_{\text{BKT}} ; t_c = (T_{\text{c0}} - T_{\text{BKT}}) / T_{\text{BKT}}$$



name	L nm	R_N Ω	I_c nA	R_0 Ω	T_{c0} K	T_{BKT} mK	b
J200-1	200	720	4	8,500	0.23		
J200-2	200	425	5				
J200-3	200	370	10	1,400	0.43	45	5.22
J200-4	200	410	50	1,000	0.5	60	9.3
J300-3	300	350	30	1,300	0.38	80	8.7
J400-1	400	650	0	16,000	0.285		
J600-1	600	440	0				

Aslamasov-Larkin
 $R_0 = 16\hbar/e^2 \sim 65 \text{ k}\Omega$

TABLE I. Main parameters for the investigated devices: name, length L , normal resistance R_N , critical current I_c at $T = 280 \text{ mK}$, mean field resistance R_0 , mean field critical temperature T_{c0} , BKT temperature, dimensionless parameter b of Eq. (2).

Large b , large $T_{c0} - T_{\text{BKT}}$

Condensation energy loss in vortex core
 \gg Superconducting stiffness

Berezinskii-Kosterlitz-Thouless
(BKT)
as in 2D-XY model



Conclusion

Josephson supercurrent observed in Al/G/Al diffusive junctions
G on SiC: a way towards more complex Graphene-based
superconducting devices

Hysteretic collapse and revival of the Josephson current:

Unique manifestation of Josephson effect
(no other example known up to date)

Vortices are present in the devices (not only in the Al itself)

at the Al/G interface

Multiple hints of BKT: hysteresis in $R(H)$, $R(T)$ fits, shape of $R(H)$,...



GRAPHENE FLAGSHIP